Triplicated P-wave measurements for waveform tomography of the mantle transition zone

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Abstract. Triplicated body waves sample the mantle transition zone more extensively than any other wave type, and interact strongly with the discontinuities at 410 km and 660 km. Since the seismograms bear a strong imprint of these geodynamically interesting features, it is highly desirable to invert them for structure of the transition zone. This has rarely been attempted, due to a mismatch between the complex and band-limited data and the (ray-theoretical) modelling methods. Here we present a data processing and modelling strategy to harness such broadband seismograms for finite-frequency tomography. We include triplicated P-waves (epicentral distance range between 14 and 30°) across their entire broadband frequency range, for both deep and shallow sources. We show that it is possible to predict the complex sequence of arrivals in these seismograms, but only after a careful effort to estimate source time functions and other source parameters from data, variables that strongly influence the waveforms. Modelled and observed waveforms then yield decent cross-correlation fits, from which we measure finite-frequency traveltime anomalies. We discuss two such data sets, for North America and Europe, and conclude that their signal quality and azimuthal coverage should be adequate for tomographic inversion. In order to compute sensitivity kernels at the pertinent high body wave frequencies, we use fully numerical forward modelling of the seismic wavefield through a spherically symmetric Earth.

1 Introduction

The mantle transition zone (MTZ) is of great interest geodynamically, since its properties determine the extent to which material and heat gets exchanged between the upper and lower mantle. In the seismological view, the MTZ extends from the discontinuity at 410 km depth to one at 660 km – both discontinuities are characterized by marked jumps in seismic velocity. The sharpness and topographic undulations of these discontinuities can be linked to mineral physics laboratory experiments in order to infer material properties and mantle rheology.

The seismic waves that sample the MTZ most extensively are regional body waves, i.e., refracted waves that turn within the MTZ. Travelling only moderate distances of Δ≈1500–3100 km (i.e. 14–29°), these waves are recorded strong and clear on seismic stations, delivering by far the highest signal to noise ratio of any wave type that could be used to study the transition zone. Yet these phases have rarely been used in general, and for seismic tomography in particular, in sharp contrast to teleseismic phases (Δ > 30°). The reason is that these regional waves generate more complex signals than teleseismic ones as they have interacted more extensively with the MTZ discontinuities. Such observations do not lend themselves to abstraction into isolated pulses and the associated, idealized modelling by ray theory. Conversely we may suspect that if we succeed at modelling and inverting these waveforms, we will be able to learn a great deal about the mantle structures that are leaving such a strong imprint on them. Here we demonstrate that this should be possible.
Regional P and S waves are commonly termed triplicated waves, since every interaction with a discontinuity spawns three distinguishable phases. We investigate triplicated P-waves, which occur at epicentral distances of $14^\circ$ to $29^\circ$, and sample the MTZ in some interval halfway between source and receiver. Our aim is to use them in finite-frequency waveform inversion for transition zone structure.

Finite-frequency modelling as originally conceived by Dahlen et al. (2000) is feasible across the entire relevant frequency range of body waves, but has been limited to interpreting direct and reflected teleseismic phases (Montelli et al., 2004; Sigl och et al., 2008; Zhou et al., 2004, 2006; Tian et al., 2011), due to the applicability limitations of paraxial ray tracing for computing sensitivity kernels. Here we present kernels that overcome this limitation. They are obtained from fully numerical forward computations of the seismic wavefield, using the spectral element code of (Nissen-Meyer et al., 2007b). Exploitation of the near-spherical symmetry of the 3-D Earth uses the currently available computational resources very efficiently, allowing access to the entire relevant broadband range of the wavefield (0.03 to 1 Hz), like the original Dahlen method.

Triplicated body waves carry a very strong imprint of their interaction with transition zone discontinuities, which is both an advantage and a challenge. Not only do the triplicated arrivals overlap each other in time, due to the finite-frequency nature of real data, but for shallow earthquakes they additionally overlap the depth phases $pP$ and $sP$, which get triplicated themselves. Hence an integral part of modelling the waveforms is the careful estimation of source parameters (since they determine the shape of the synthetic Green’s function), and of the source time function.

The differential moveout of the triplicated phases has since long been used to derive one-dimensional velocity models (Grand, 1984), which required a large number of seismic stations in a narrow azimuth range. Modelling of individual triplicated waveforms has been successfully used to sample localized heterogeneities in the MTZ (Tajima and Grand, 1995; Melbourne and Helmberger, 2002; Tajima et al., 2009). A few studies that included picked arrival times into ray theoretical inversions demonstrated the potential of triplicated waves for tomography (Grand, 2002), but so far they have rarely been used. Only very recently, Zhu et al. (2012) used triplicated phases, amongst others, for a European regional tomography, albeit at lower frequencies.

Regional body waves are complementary to all phases currently used for MTZ studies. Teleseismic body waves also offer good signal-to-noise ratios, but have comparably low sensitivity in the MTZ, which they traverse at steep angles. Hence they constrain the MTZ beneath sources and/or station, whereas triplicated waves sample it extensively midway between sources and receivers. So it would be highly beneficial to combine them in one inversion.

Other methods for sampling transition zone discontinuities have much lower signal-to-noise ratios (SNR). Receiver functions exploit P-to-S or S-to-P converted energy of body waves, which require stacking numerous seismograms. Their migration from the time domain to depth depends on a velocity structure model, which either must have been obtained independently or is neglected, with corresponding systematic errors in the result.

PP and SS precursors, i.e., body waves reflected at the undersides of MTZ discontinuities, have also been used in structural studies, (Shearer and Masters, 1992; Thomas and Billen, 2009; Deuss et al., 2006; Deuss, 2009). Their SNR is low, so that only the rare strong earthquakes that are recorded on seismic arrays can be used. Distinguishing between the signal of an undulated discontinuity and a volumetric velocity perturbation is challenging (Chaljub and Tarantola, 1997), as for receiver functions.

Surface waves have lower image resolution than body waves. Only their higher modes have significant sensitivity to the MTZ, but higher modes carry little energy, and are more difficult to process. Hence surface wave tomography is largely limited to depths above the MTZ.

We start with a discussion of the nature of triplicated body waves, and of their expression in actual seismic broadband data (Sect. 2.1). Section 2.2 and 2.3 demonstrate how we model these waveforms; this covers the computations of Green’s functions and the inversion for source time functions and source mechanisms. We then explain the concept of wavefield kernels (Sect. 3), and show how passband-filtering to different frequency bands significantly increases the resolution in the transition zone, by comprehensively exploiting information across the entire broadband range (Sect. 3.3). The sizeable and well-instrumented continents of Europe and North America currently offer the most favourable source-receiver combinations of criss-crossing regional body waves for tomography. Section 4 discusses the two data sets that we have assembled for these two regions, with a focus on the USArray. We conclude with a discussion of the results, and the prospects of inverting these data for MTZ structure (Sects. 5 and 6).

## 2 Regional P-waves

### 2.1 Triplications

The term triplication refers to three seismic wave phases that have similar ray parameters and arrive closely spaced in time. The concept is rooted in ray theory. While our data processing and kernel computations are targeted at interpreting the full waveforms, it is useful to consider their ray theoretical approximation first, in order to appreciate the nature of triplicated waves. It assumes that the wave from one source to one receiver travels along an infinitesimally narrow ray path, which is described by the eikonal equation (e.g., Kennett,
Strictly speaking, the approximation only holds for the case of a non-dispersive medium. Even when the medium is not intrinsically dispersive, velocity heterogeneities may introduce a frequency-dependent group velocity, which is the motivation for finite-frequency tomography.

In a layered velocity model \( c(r) \), the traveltime \( \tau \) and the angular distance \( \Delta \) of a direct phase (e.g., a P-wave) depend only on the ray parameter \( \varphi \).

\[
\Delta(\varphi) = \int \frac{dr}{r \sqrt{r^2/(\varphi c(r))^2 - 1}}
\]

(1)

\[
\tau(\varphi) = \int \frac{dr}{c(r) \sqrt{1 - (\varphi c(r))^2/r^2}}
\]

(2)

If the velocity profile contains strong gradients, or even discontinuities with positive velocity jumps, \( \frac{dc}{dr} \) changes sign, so that rays of smaller \( \varphi \) arrive closer to the source\(^1\). Because \( \frac{d\tau(\varphi)}{d\varphi} < 0 \) in either case, two rays arrive at the same distance at different times. If \( \frac{dc}{dr} < 0, \Delta(\varphi) \) is still continuous. The turning points of \( \Delta(\varphi) \) mark the transition (with decreasing \( \varphi \)) first from a ray travelling above the discontinuity to one being critically reflected at the discontinuity and then to one travelling below it. In the traveltime-distance relation \( \tau(\Delta) \), which is also continuous, a pattern called triplication emerges (Fig. 2).

\(^1\)The literature does not provide any hard constraints for a triplication to occur. However, it is clear that a discontinuity in \( c(r) \) or \( dc/dr \) will be sufficient.
The velocity discontinuities in seismic velocity in the upper mantle (at 410 and 660 km depth in the IASP91 reference model (Kennett and Engdahl, 1991), henceforth termed 410 and 660, produce triplications: Neglecting crustal phases and the weakly developed 210-km discontinuity, we receive one P phase up to a distance of 14°, which has travelled through the upper mantle. At 14° another P-phase arrives 8 seconds later (point D in Fig. 2), being reflected at the 410. This branch bifurcates into one reflected path (DC), and one refracted below (DE). The refraction branch continues to 28° distance (E), while the uppermost-mantle branch meets with the reflected one at 21.5° (C) and ends there. From 17.5° (F) on there are also reflection and refraction branches from the 660. The 660-reflection branch (EF) meets with the 410-refraction branch (DF) at 27.8° (E), where they both end. Only the 660 refraction branch can be measured at distances exceeding 27.8°.

With this conceptual knowledge, consider the real data in Fig. 1. It shows broadband P-waves in a 20 s window, starting 5 s before the first arrival predicted by IASP91. The 692 waveforms from stations in the western United States are aligned (VanDecar and Crosson, 1990) and clustered by similarity as described by Sigloch and Nelet (2006). This clustering results purely from the waveform shapes and does not use meta-information such as station distance or azimuth from the source. The clusters show a clear zonation by distance, caused by the triplications from the transition zone discontinuities. The figure can best be understood by first considering the most distant group of P-waves (pink). The stations are mainly located beyond 28° epicentral distance, so that the signal contains no triplications. The secondary pulse, arriving 7 s after the first one, can therefore be recognized as a reflection from the ocean surface near the source (pwP).

In the distance bin closest to the source, from ≈15° to 18° (red), the triplicated phases overlap so that just one broadened pulse arrives. In the second group (yellow), the arrivals are further spread so that a first arriving pulse, a surface reflected phase (at 5 s) and multiple triplicated phases can be distinguished. Additionally, we observe an arrival ≈10 s after the first one, which is a reflection from the 660 (FE branch in Fig. 2). In the third group (green), this reflection is already closer to the first arrival, and the first-arriving pulse is a superposition of the DE branch from the transition zone and the BC phase from the upper mantle and depth phases. The next group (dark blue) is quite heterogeneous and marks the transition from 410 triplications to 660 triplications.

In the cyan group, beginning at 22°, the refractions above and below the 660 arrive almost at the same time and collapse into a single pulse. The reflected phase is usually quite weak and not visible at all here. The two clearly separated arrivals hence correspond to P (two overlapping refractions) and pwP (another two refractions). In the next two groups (gray green and purple), the refracted phase from above and below the 660 begin to separate, so that they spill into pwP once more. The most distant group (pink) shows clearly separated P and pwP pulses no longer affected by triplications. The shape of this teleseismic waveform does not change much out to ≈85° distance.

Hand-picked arrival times of the different triplication branches have been used in a few tomographic studies (Grand, 1994, 2002), although this approach fails to take into account the finite frequencies of seismic waves. As Fig. 1 demonstrates, the triplications are often not clearly separated,
due to several factors. The finite duration of the source rupture has a low-passing effect. Earth’s intrinsic attenuation disperses the P-wave pulse, which does not contain much energy above 1 Hz. Additionally, waves of a finite wavelength $\lambda$ are influenced by scatterers off of the direct path, if the detour to reach the scatterer is less than $\lambda/2$, which is the definition of the Fresnel zone. This argument is continued in Sect. 3.

### 2.2 Waveform modeling

We download broadband seismograms from the IRIS and ORFEUS data management centres. The waveforms are corrected are band-passed between 0.01 Hz and 3.5 Hz, detrended, and transferred to ground displacement by deconvolving the instrument responses. A time window is cropped from 10 s before to 25 s after the theoretical P arrival. Noisy seismograms are singled out by a clustering algorithm and removed manually.

In order to do cross-correlation measurements for waveform tomography, it is necessary to compare a synthetic waveform to the observed seismogram. Synthetic seismograms are calculated using the reflectivity method of Fuchs and Müller (1971). As a reference model we use IASP91 (Kennett and Engdahl, 1991), together with the density and intrinsic attenuation of PREM (Dziewoński, 1981).

Fig. 3 demonstrates the challenge of modelling regional P-waves. Within a short time window, three to five triplicated phases arrive (Fig. 3a). If the earthquake is shallow, as most earthquakes are, the surface-reflected phases sP, sP or pwP arrive within a few seconds of P, and are themselves triplicated (Fig. 3b). For an earthquake at 20° epicentral distance, ten phases arrive within less than 9 s, triplicated by both the 410 and the 660 discontinuities. The polarity of the reflected phases is negative compared to the refracted phases, and the depth phases may have reversed polarity depending on the source plane orientation. Hence the overall waveform is highly sensitive to the exact depth, mechanism, and distance of the earthquake.

Additionally, the finite duration of the source process is imprinted on the seismogram, which is the convolution of the moment rate function $\dot{m}(t)$, termed source time function (STF), with the Green’s function $G(r_s, r_e, \tau)$. Since duration of the STF is usually of several seconds, it can change the waveform completely.

If the maximum frequency in the seismgrams is $f \ll 1/T$, where $T$ is the duration of earthquake rupture, then the source time function is sometimes approximated by a Dirac delta, a triangular function or a Gaussian. This is usually done in surface wave tomography and long-period waveform inversion. We use earthquakes of moment magnitudes between 5.5 and 7.0, where $T$ is between one and several tens of seconds, and we want to invert up to dominant periods of up to 1 s. Hence this approximation is too rough for our purposes, and we need explicit estimates of each STF in order to construct the matched filter.

![Flowchart of the source inversion procedure as described in (Sigloch and Nolet, 2006).](#)

### 2.3 Source inversion

As seen in the previous section, waveform tomography requires an inversion for the temporal and spatial parameters of the earthquake sources prior to the actual tomographic inversion. For the deconvolution of the STF, we use teleseismic P-waves rather than the complex, triplicated regional waves. We briefly describe the procedure here and in Fig. 4, for details see Sigloch and Nolet (2006): We remove obviously problematic stations and align all waveforms to the arrival of the P-phase (VanDecar and Crosson, 1990). We then choose a reasonable candidate depth range to survey, 1–50 km for shallow events and NEIC depth ±30 km for deep events. Then we execute the following scheme for each candidate depth: First a joint deconvolution of the synthetic seismograms, calculated with the NEIC moment tensor $M_0$ from the measured seismograms is done, resulting in an STF estimate $\dot{m}(\tau)$. Source orientation is assumed to be constant during the rupture, so that $\dot{m}(\tau)$ is identical for all components of the moment tensor. Second, with this STF, an update for the moment tensor $\delta M$ is calculated and the amplitudes of all stations are corrected individually. The new moment tensor $M_0 + \delta M$ and the amplitude corrections are used to derive a new STF estimation and this is repeated, until the
RMS misfit between synthetics and broadband seismograms has converged.

After all depths have been treated, we manually choose the depth, at which the RMS misfit is minimal and the STF does not contain any significant negative parts, which would be unphysical. The STF and moment tensor results for this “most likely” depth are retained for kernel calculation and tomography.

The teleseismic Green’s functions are calculated by the WKBJ code of Chapman (1978), using IASP91 as reference model. For source inversion we use only waveforms from globally distributed, reliable broadband stations (GSN and Geoscope networks). For typical earthquakes, around 40 of these stations are located within teleseismic range. Since STF deconvolution is a numerically sensitive operation, we deliberately use only this small, high-quality ensemble, rather than all available broadband stations. The spatial distribution of these permanent, international network stations is relatively even, whereas a deconvolution from all IRIS stations would always be dominated by the 1000+ receivers located in North America. Their waveforms and misfits are highly correlated, so that the additional information content with regard to the source is low. However, all available stations will later be used for tomography.

We always attempt to invert for a single STF that fits all global teleseismic data, but in about one out of three earthquakes, we need to allow for two or more regional STF solutions, e.g., when the European station cluster cannot be fit to the same STF as the North American cluster. This may be due to structure close to the source, like a subducting slab or be an effect of source directivity. Our view of a “source time function” is pragmatic: we want it to absorb all signal that is common to all seismograms, even when that signal does not derive from the source rupture sensu stricto. The remaining signal can then be interpreted as an imprint of the structure along the wave-path.

3 Sensitivities

3.1 Waveform tomography – direct phases

The concept of arrival time of a phase, which may be picked manually by an analyst, assumes a broadband minimum-phased signal. In a heterogeneous Earth, scattering off of the “direct” path adds a small, frequency-dependent component to the direct waveform. Hence scattering introduces a non-linear dispersion even if the medium is perfectly viscoelastic (Dahlen et al., 2000; Nolet, 2008). This dispersion reflects the scale-dependent interaction of different finite wavelengths with the mantle heterogeneities that we want to image. Hence it embodies the information that waveform inversion captures above and beyond the ray theoretical approximation. We measure this dispersion by the method of matched filtering (Sigloch and Nolet, 2006).

A predicted waveform \( u(t) \) is synthesized from six partial Green’s functions \( G_j(r_x, r, t) \), weighted by the six independent components of the moment tensor \( M_j \), and convolved by the source time function \( \dot{m}(t) \). The broadband \( u(t) \) is immediately bandpass filtered to \( u_k(t) \), through convolution with a filter response \( f_k(t) \) (\( k \) is the frequency band index). Hence the finite-frequency synthetic is

\[
u_k(t) = \sum_{j=1}^{6} G_j(r_x, r, t) \cdot \dot{m}(t) \cdot M_j \cdot f_k(t),
\]

which must be compared to an accordingly filtered observed waveform \( u_k^o(t) \). For this we parametrize \( u_k(t) \) by the two observables (misfit measures) that we want to estimate: the traveltime anomaly \( \delta T_k \) and the amplitude anomaly \( \delta A_k \).

\[
\hat{u}_k(t) = A_k u^o(t - \delta T_k).
\]

\( \hat{u}_k(t) \) is the matched filter, and the optimal \( \delta T_k, \delta A_k \) are obtained by minimizing the RMS misfit between \( \hat{u}_k(t) \) and \( u_k^o(t) \). This is equivalent to finding the time shift \( \delta T \) that maximizes the cross correlation between \( \hat{u}_k(t) \) and \( u_k^o(t) \).

With this method, we obtain up to 2-6 frequency-dependent misfit observables \( \delta T_k, \delta A_k \) from one broadband P-wave seismogram. The derivative of these misfits with respect to the Earth model can be expressed in so-called sensitivity kernels \( K_k(x) \). These represent the sensitivity of the traveltime misfit or the amplitude misfit with respect to changes in P-wave velocity \( \Delta V_P / V_P \) at a given point \( r_x \). The traveltime anomaly \( \delta T_k \) is then modelled as

\[
\delta T_k = \int_{\Omega} K_k(x) \frac{\Delta V_P}{V_P}(r_x) \, d^3r_x.
\]

Obviously, this kernel has to be calculated using a reference velocity model. Equation 5 and the construction of the kernel \( K_k \) contain the assumption that the traveltime anomaly \( \delta T_k \) originates exclusively from single scattering off of anomalies \( \Delta V_P / V_P \), which quantify the difference between the reference model and true Earth structure. This so-called Born approximation is justified by the observation that the magnitude of lateral mantle heterogeneities \( \Delta V_P / V_P \) is small, typically on the order of a few percent, so that multiple scattering can be neglected. Kernel \( K_k \) is the first Fréchet derivative of \( \delta T_k \) towards \( \Delta V_P(r_x) \) (Marquering et al., 1999).

Dahlen et al. (2000) proposed a fast algorithm to derive kernels for teleseismic body waves by paraxial ray tracing. This effectively uses ray theory to go beyond the limits of ray theory, since it synthesizes sensitivity kernels of finite volume from the interaction of an infinity of rays. The method has been applied to teleseismic body waves with great success (Montelli et al., 2004; Sigloch et al., 2008) and was extended to surface waves (Zhou et al., 2004, 2006; Tian et al., 2011) but its scope is limited to phases without caustics, diffractions or other wave effects (Dahlen et al., 2000; Nissen-Meyer et al., 2007a).
3.2 Waveform tomography – arbitrary phases

Triplcated waveforms, with their interactions of refracted and reflected phases around the discontinuity, are not adequately modelled by the ray theoretical formalism. The caustics at turning points A–F (Fig. 2) would lead to infinite amplitudes at the corresponding distances. Moreover, the ray-centred approach by Dahlen et al. (2000) works strictly speaking only in a continuous velocity model. Hence we need to calculate the kernels from the full waveform instead.

Computing the first order perturbation \( \delta \mathbf{u}(t) \) of a seismic waveform \( \mathbf{u}(t) \) involves the waveform from source to every possible scattering location \( \tilde{\mathbf{u}}(t, \mathbf{r}) \), and of the scattered waveform to the receiver. Thanks to source-receiver reciprocity, this second waveform may instead be replaced by the back-propagating waveform \( \tilde{\mathbf{u}}(t, \mathbf{r}) \) from receiver to scatterers, which is generally much cheaper computationally (Nissen-Meyer et al., 2007a, eqn. 10). This is conceptually similar to the adjoint method (Tromp et al., 2005).

\[
\delta \mathbf{u} = -\oint \left[ \frac{\partial}{\partial \mathbf{r}} \tilde{\mathbf{v}}_i \cdot \tilde{\mathbf{v}}_i + \tilde{E}_{ij} \cdot \tilde{E}_{kl} \delta C_{ijkl} \right] d^3 \mathbf{r}. 
\]

\[
\tilde{\mathbf{v}} = \delta \mathbf{u} \text{ is the velocity field of the forward propagating wave and} \\
\tilde{E}_{ij} = \frac{1}{2} \left[ \frac{\delta \mathbf{u}_i}{\delta r_j} + \frac{\delta \mathbf{u}_j}{\delta r_i} \right] \text{ is the strain tensor. Note that this is} \\
\text{index notation, so summation over repeat indices is implied.} \\
The arrows serve as a reminder of the forward and backward nature of the wavefields and strains. For an isotropic medium, the dependence on the Lamé parameters is

\[
\delta \mathbf{u} = -\oint \left[ \frac{\partial}{\partial \mathbf{r}} \tilde{\mathbf{v}}_i \cdot \tilde{\mathbf{v}}_i + \tilde{E}_{ii} \cdot \tilde{E}_{ii} \delta \lambda + 2 \tilde{E}_{ij} \cdot \tilde{E}_{ij} \delta \mu \right] d^3 \mathbf{r}. 
\]

If the inversion is for \( \delta V_p \) and \( \delta V_S \) rather than for the Lamé parameters \( \delta \lambda, \delta \mu \), we replace them:

\[
\delta \mu = V_S^2 \delta \rho + 2V_S \rho \delta V_S 
\]

\[
\delta \lambda = \left( V_P^2 - 2V_S^2 \right) \delta \rho + 2V_P \rho \delta V_P - 4V_S \rho \delta V_S 
\]

Replacing \( \delta \mu \) and \( \delta \lambda \) in Eq. (7), we have

\[
\delta \mathbf{u} = -\oint \left[ \frac{\partial}{\partial \mathbf{r}} \left( \tilde{\mathbf{v}}_i \cdot \tilde{\mathbf{v}}_i + \left( V_P^2 - 2V_S^2 \right) \tilde{E}_{ii} \cdot \tilde{E}_{jj} + V_S^2 \tilde{E}_{ij} \cdot \tilde{E}_{ij} \right) \right] d^3 \mathbf{r} \\
+ \delta V_P \left( 2 \rho \tilde{E}_{ii} \cdot \tilde{E}_{jj} \right) \\
+ \delta V_S \left( -4 \rho V_S \tilde{E}_{ii} \cdot \tilde{E}_{jj} + 2 \rho \tilde{E}_{ij} \cdot \tilde{E}_{ij} \right) d^3 \mathbf{r}. 
\]

Equation 11 shows that \( \delta V_p \)-kernels are straightforward to calculate because they only involve the diagonal elements of the strain tensor, which is equivalent to the divergence of the displacements: \( \tilde{E}_{ii} = \frac{\partial \tilde{u}_i}{\partial r_i} = \nabla \tilde{u} \). Hence for P-wave tomography, we need to store only the displacement field \( \mathbf{u}(r) \), rather than the full strain tensor \( \tilde{E}_{ij}(r) \). The exact expression of the kernel now depends on the chosen misfit criterion. We prefer the cross-correlation traveltime misfit measured on one component \( i \) (in the case of P-waves usually BHZ), defined as

\[
\delta T = -\Re \int_0^\infty \frac{\omega \tilde{u}_{ij}(\omega) \delta \mathbf{u}_i(\omega) d\omega}{\int_0^\infty \omega^2 \tilde{u}_i(\omega) \tilde{u}_i(\omega) d\omega}. 
\]

With \( u_i(\omega) = G_{ij}(r_s, r_o, \omega) \tilde{m}(\omega) M_j \), we can calculate the sensitivity of \( \delta T \) w.r.t. \( \delta V_P \). Using the definition of the kernel in Eq. (5), we arrive at

\[
K(r_s) = \sum_{j=1}^6 \int_0^\infty \frac{2V_P(r_s) \rho(r_s)}{\omega^2 |G_{st,ij}(\omega)\tilde{m}(\omega)|^2} \cdot M_j \\
\cdot \Re \int_0^\infty \frac{\omega G_{st,ij}(\omega) \tilde{m}(\omega)}{\omega} d\omega. 
\]

The term \( \tilde{m}(\omega) \), which Dahlen et al. (2000) originally denoted as the source term, contains the source spectrum, but also the bandpass filters, \( G_{st}(\omega) \), the Green’s function from source to receiver, introduces any intrinsic attenuation of the reference Earth model into the kernel.

3.3 Spherical Earth kernels

The calculation of a global waveform at a dominant period of 5 s requires around \( 10^4 \) CPUh when a full 3-D forward solver like SPECFEM (Komatitisch and Tromp, 2002) is used. For a realistic iterative global tomography using >10⁵ waveforms, the calculation cost would be \( \gg 10^9 \) CPUh, which is completely prohibitive. In a spherically symmetric background model, this cost can be reduced dramatically: 3-D wavefields in a layered Earth can be computed at the cost of the equivalent 2-D wavefields, since the symmetry implies that one dimension may be calculated analytically (Nissen-Meyer et al., 2007a). Forward wavefields are pre-computed for reasonable depth increments (e.g. increments of 1 km for depths from 0 to 100 km, and increments of 10 km from 100 to 700 km, requiring 160 simulations). The backward wavefield needs to be calculated just once, assuming that all receivers are located at the surface or within one P-wavelength of it. The 160 forward calculations need to be done four times (Nissen-Meyer et al., 2007a, p. 1057) for

1. a \( M_{zz} \) monopole source
2. a \( \frac{1}{2} (M_{xx} + M_{yy}) \) monopole source
3. a \( M_{xz} \) dipole source
4. a \( M_{xy} \) quadrupole source.
Fig. 5. Traveltime sensitivity kernels for \( \Delta V_p/V_p \), calculated by the Axisem spectral element code. Sensitivities are for a cross-correlation traveltime misfit, in the time window of 5 s before to 15 s after the estimated arrival. Dominant period is 10 s for the upper two rows, and 20 s for the lower two rows. Distances (from top left): 22°, 24°, 26°, 30°, 35°, 40°. Background model: IASP91; source: explosion; receiver: z-component. The 410-discontinuity is marked by the dashed line, the 660 by the dashed-dotted line. Note that most kernels do not feature the famous doughnut hole, which is filled in by the sensitivities to the two discontinuities.

Fig. 6. Nominal ray paths of first arriving P-waves in IASP91. None of the rays bottom out in the lower part of the transition zone. Contrast this to the realistic (finite-frequency) sensitivities of Fig. 5, which extend broadly across the entire MTZ.

Since the response of a station at azimuth \( \phi \) to a \( M_{x2} \)-source equals that of a station at \( \phi - \pi/2 \) to a \( M_{y2} \)-source, and response of a \( (M_{xx} - M_{xy}) \)-source at \( \phi \) equals that of a \( M_{xy} \)-source at \( \phi - \pi/4 \), we can reconstruct the response of a spherically symmetric Earth to an arbitrary moment tensor from these four calculations. The backward propagation needs to be done twice:

1. \( p_x \) monopole source for the Z-component of the seismogram
2. \( p_x \) or \( p_y \) dipole source for the E- or N-component of the seismogram

Again, \( p_x \) or \( p_y \) are equivalent if the receiver location is rotated by \( \pi/2 \). Using the 3-D to 2-D reduction strategy applied in the SEM-code Axisem (Nissen-Meyer et al., 2007b, 2008), the computation cost for a 3-D global waveform of dominant period \( T = 5 \) s is around 16 CPUh on an i7 machine, or \( \approx 10^4 \) CPUh for the entire wavefield library. Since the calculation grows at \( O(1/T^3) \), a library of dominant period 1.25 s would still require less than 10^6 CPUh, which is easily feasible nowadays. From these 642 pre-computed wavefields, kernels for any arbitrary time window in the seismogram can be calculated on the fly in the frequency domain, which is memory intensive but computationally cheap.

Time window choices for these kernels are not limited to any specific phase arrivals or wave types, although it is certainly judicious to choose parts of the seismogram that contain significant seismic energy rather than noise. The window
length should be chosen with care. A window that is too long will contain more noise than necessary, and the diameter of the kernel will grow, since longer detours from the direct path are allowed. The outer parts of the kernel will contain the higher-order Fresnel zones, which oscillate rapidly and are unlikely to meaningfully contribute in the inversion. Windows too short will contain too little signal and be more prone to cycle skips. The window length should probably be no shorter than twice the dominant period of the bandpass filter. It will not be possible to calculate kernels separately for each of the triplicated phases, since in real data they overlap in time (cf. Fig. 3). However, it is neither necessary or even desirable to revert to this Dirac-type, ray-theoretical way of processing. The kernel formalism ensures the proper interpretation of the waveforms, as long as the actual measurements use the same window lengths and filters as the waveform computations.

3.4 Kernel gallery

A selection of $V_p$-kernels at dominant periods of 10 s and 20 s are plotted in Fig. 5, for an explosive source at the surface and the z-component of the seismogram. Especially at 24° epicentral distance, the two frequency bands differ significantly in their sampling of the MTZ. While the 20 s kernel samples the regions directly below the 410 and the 660, the 10 s kernel samples mainly the region above the 660. This is particularly striking when compared to the sensitivity of the first arriving rays (Fig. 6), which is completely confined to the region directly below the discontinuities. The 22° and 26° kernels in the 10 s band have nearly complementary sampling characteristics in the transition zone. The 22° kernel is negative where the 26° one has its largest positive values. With dense arrays like the USArray, we obtain many 22° and 26° recordings for the same earthquake, which thus should yield good constraints on the MTZ. The 30° to 40° kernels in the second and forth row look more similar to teleseismic kernels, even though clear imprints of the MTZ remain even for a 40° kernel, resulting in an appearance quite different from the 40° kernel of the original Dahlen method (Dahlen et al., 2000). Geodynamically interesting regions just above the discontinuities, where effects of fluid release might be present (Ohtani, 2005), can classically be sampled only by teleseismic waves. Since they traverse the MTZ at steep incidence angles, their vertical resolution is quite limited, in contrast to triplicated phases. Topography on the discontinuities may also influence the waveforms, an effect for which sensitivities may be computed from the same wavefields (Nissen-Meyer et al., 2007a; Colombi et al., 2012). Ultimately it will be desirable to separate topography effects from those of the volumetric velocity structure, by integrating both kinds of kernels into a joint inversion.
4.1 North America

Since the advent of USArray, North America is clearly the best-instrumented landmass on Earth. USArray stations are spaced by \( \approx 70 \text{ km} \) on a regular grid and deliver superb broadband waveforms.

The data from the first year of instalment already brought new insights into the subduction history of the Farallon plate and the formation of the Rocky mountains (Sigloch et al., 2008) or to fluid transport in the Gorda subduction system (Cao and Levander, 2010). The recent move of the deployment into the Great Plains has brought the seismocities of the Guerrero subduction and along the western Canadian margin into distances of 15° to 30°, creating large numbers of crossing paths in triplication range. USArray recordings are supplemented by permanent networks in the US, Canada, and Mexico, and by data from temporary experiments. All North American data was downloaded from the IRIS data management center (DMC). Currently IRIS delivers about 2000 global stations per event, of which \( \approx 1400 \) are located in larger North America, i.e. between 180° W and 45° W in the Northern Hemisphere.

We found that between 01/01/2001 and 31/12/2011, 92 regional earthquakes generated triplicated P-wave recordings of acceptable signal-to-noise ratio. This yielded 26 016 unique, acceptable wave paths and broadband waveforms in total. We applied Gabor bandpass filters (bandwidth one octave) at centre periods of 20 s, 10 s, 5 s, 2.5 s, 1.25 s. Since we make cross-correlation measurements, the correlation coefficient between observed (filtered) waveforms and their synthetics using IASP91 serves as the primary measure of goodness of fit. We denote by \( \delta T \) the time shift that maximizes the cross-correlation between observed seismogram and matched filter as in Eq. (4), and by \( CC_{\text{max}} \) the correlation coefficient at this optimum time shift. Hence \( CC_{\text{max}} \) acts as a quality measure, and \( \delta T \) is the actual finite-frequency observable to be interpreted by tomography. Previous experience (Sigloch and Nolet, 2006; Sigloch, 2008) lets us assume that \( CC_{\text{lim}} \geq 0.8 \) is a good threshold for acceptance. If we only accept filtered waveforms with \( CC_{\text{max}} \geq 0.8 \), 42 949 out of 130 080 remain (Table 1). Fitting waveforms in the five separate frequency bands thus increases the number of usable data more than fourfold, compared to fitting only the broadband seismograms. In particular, we can often accept at least one passband measurement even when the \( CC_{\text{max}} \) of the broadband measurement is clearly too low – this salvages many important wave paths. For teleseismic waves, another frequency band below 20 s might reasonably be added, but for regional P-waves this is less interesting, since the 20 s kernels already fill up the entire depth range of the transition zone (see Fig. 5).

Figure 8 shows a comparison between matched filters and real waveforms for the seismograph station at Mount St. Helens crater, which is by no means an ideal station. Still three out of five bands have \( CC_{\text{max}} > 0.8 \) and could contribute to tomography. These seismograms were calculated using IASP91 velocity model. For an actual tomography of North America it may be beneficial to calculate matched filters and kernels in a regional 1-D model; for a recent model and a comparison between previous results see Chu et al. (2012).

Figure 9 shows that the average absolute traveltime anomaly \( \delta T \) is similar in all bands, with a standard deviation of \( \approx 2.4 \text{ s} \). From our experience with teleseismic P-waves, we know that a large part of this \( \delta T \) signal is due to mislocated sources rather than to mantle heterogeneity; both contributions are jointly inverted for by our tomography software.

These \( \delta T \) measurements on triplicated data will be embedded into a larger data set of teleseismic P-wave data (Sigloch, 2011). The latter have better azimuthal coverage, since they include earthquakes from the east (mid-Atlantic ridge and southern Europe). Unfortunately, very few seismic sources east of North America are located at regional distances.
Table 1. Number of acceptable traveltime measurements in the various frequency bands, as a function of the chosen rejection threshold $CC_{lim}$. In total 26016 (NA) and 4916 (Europe) broadband seismograms were available.

<table>
<thead>
<tr>
<th>Frequency Band</th>
<th>Northern American data set</th>
<th>European data set</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$CC_{lim}$</td>
<td>0.70</td>
</tr>
<tr>
<td>20 s</td>
<td></td>
<td>19897</td>
</tr>
<tr>
<td>10 s</td>
<td></td>
<td>17646</td>
</tr>
<tr>
<td>5 s</td>
<td></td>
<td>12691</td>
</tr>
<tr>
<td>2.5 s</td>
<td></td>
<td>8180</td>
</tr>
<tr>
<td>1.25 s</td>
<td></td>
<td>3561</td>
</tr>
<tr>
<td>total</td>
<td></td>
<td>61975</td>
</tr>
<tr>
<td>broadband</td>
<td></td>
<td>14552</td>
</tr>
</tbody>
</table>

4.2 Europe

Compared to North America, the European seismic networks are less homogeneous, even though the NERIES initiative brought a great advance. We downloaded our waveforms from the ORFEUS DMC. This archive currently contains around 400 seismic stations, mainly in Europe, but also several temporary installations by European agencies, e.g. in Indonesia. Figure 7 shows that data coverage is quite uneven. Several large countries like France and Poland are sparsely instrumented, other networks do not share their data yet. There have been several large temporary installations in Central Europe and Scandinavia, data which would be very interesting but are being released only slowly. The IRIS DMC holds hardly any broadband stations above and beyond the ORFEUS DMC. On the other hand, the geometry and seismicity of Europe is more favourable than for North America. Hellenic seismicity is recorded over a large azimuthal range from Spain to Russia and produces many crossing paths, together with Western Mediterranean seismicity recorded in Central Europe, and seismicity on the North Atlantic ridge between Iceland and Svalbard. One of the most interesting features in the transition zone are the slab remnants below the Northern Balkans and the Carpathians, which cannot be easily connected to the established subduction regimes. Sampling of the MTZ by triplicated waves is very good in this region, and should help in further illuminating its mantle processes. A clear difference to the North American data is that few earthquakes above magnitude 6 are recorded in Europe. Since we obtain best correlations between data and synthetics at around magnitude 6.5, the data quality is generally lower than in North America. In total, the number of available stations in larger Europe (defined as the region between 45° W and 75° E in the northern hemisphere) is 390. Our dataset contains 66 earthquakes, which recorded 4916 broadband seismograms (unique wave paths). 7042 out of 24 580 passband measurements have a data-synthetic fit that exceeds $CC_{\text{max}} > 0.8$. Compared to the North America, we obtain about five times fewer waveforms, and seven times fewer acceptable $\delta T$ measurements. This lower average signal quality seems to be mainly due to the weaker seismicity around Europe.

4.3 Information content of triplicated P-waves

Before embarking on tomographic inversions, we want to convince ourselves that triplicated waveforms do indeed contain coherent and usable structural information. The broad footprint of USArray may be sliced up into dense seismic profiles at various back-azimuths, each featuring dozens of stations. Here we consider one such quasi linear section, generated by an earthquake from Guerrero, Mexico. Figure 10 shows the P-waveforms of 84 displacement seismograms in a range between 22 and 35° distance. The traces are color coded, where green means zero displacement, blue is negative displacement, and red is positive. Traces are time-aligned on the IASP91-predicted arrivals of the first P-phase.

The first arrival in the real seismograms occurs around +2 s for all traces, a systematic bias w.r.t. to IASP91 that is most likely due to source mislocation. The blue triangular move-outs (e.g. to +7 s at 21° distance) are the triplicated phases of
Starting at +10 s, the whole P-arrival sequence is “echoed” (also in blue) – this is the depth phase pP, in itself triplicated, for this shallow event (12 km deep).

If the Earth were truly spherically symmetric, the P-arrivals would be aligned smoothly – if not along a vertical line of $t = 0$, then along some other smooth line of steep move-out. This is clearly not the case, signalling the kind of lateral mantle heterogeneity that seismic tomography targets. Strong unevenness is for example observed between 25 and 31° distance, where the P-onset varies between 0 s and +3 s.

The largest delays are present between 29 and 31° distance. This might be explained by a low-velocity anomaly directly below the 660, since only waves of this distance range bottom there (see Fig. 6). Recordings at more distant stations would be less influenced by this hypothetical anomaly, since they traverse it at a steeper angle, with correspondingly lower sensitivity. However, a second observation leads to another explanation: The second triplication (here arriving at $\approx 5$ s at 28°), represents the phase bottoming directly above the 660. According to IASP91, it should be recorded only to a distance of 27.8°, but here we observe it to distances exceeding 29°. This could be explained by a depression of the 660-km discontinuity to a depth of 680 km, which would also explain the delay of the first phase at this distance. A depressed 660 in this region of subduction is plausible, since the lower temperatures of the slab would shift the phase transition to higher pressures and deeper depths. Indeed, studies from SS precursors Houser et al. (2008) showed a 660 depressed to 668–671 km in Northern Mexico.

The second subplot of Fig. 10 shows several stations at 28 to 29° distance, where the second triplication should not be recorded. We do observe the phase, but only at some of the stations (at +4 to +5 s), which suggests that the depression of the 660 is quite localized. From the azimuthal spread of the stations, we can estimate their bottoming points to be spaced only by tens of kilometres, and yet the imprint of the 660 in the seismograms is quite variable. Since the maximum frequencies in these waveforms are less than 1 Hz, the scale of the undulations on the 660 must be close to the resolution limit of these waves. The aforementioned precursor study lacked the resolution to resolve such small features.

5 Discussion

Using triplicated P-waves fills an important gap in waveform tomography. Teleseismic waves have relatively poor depth resolution in the MTZ, and little sensitivity to the discontinuities themselves. Since regional waves have this resolution, we hope to greatly increase the resolution of future P-wave models in the transition zone. So far, triplicated body waves have hardly ever been used for tomography, since they are not well modelled by classical ray theory. The appearance of the actually measured waveform has a clear finite-frequency character rather than resembling a sequence of Dirac pulses.

Our choice of misfit criterion is the cross-correlation traveltime – effectively a phase shift measurement, given our relatively narrow pass-bands. Cross-correlation is the optimal strategy for the detection and estimation of a known signal (the synthetic waveform or “matched filter”) in a noisy version of the same signal (the measured waveform), where the noise is assumed to be white additive Gaussian noise in each.
passband. Intuitively it might seem that cross-correlation may not be a suitable misfit for triplicated waves, since for all but the highest frequencies, the time window will necessarily encompass all three triplicated phases, each of which has different spatial sensitivity. Hence calculating one traveltime delay on all three overlapping phases may seem unphysical. We believe that this understanding of the cross-correlation misfit is misguided by (ray-theoretical) intuition. While it is true that one cross-correlation applied to a broadband signal only calculates one delay time for the whole broadband time series, this is actually not what we propose to do. When splitting the signal into multiple frequency bands \( k \) and calculating separate \( \delta T_k \), several, ideally independent measurements are done on the waveform. The corresponding sensitivity kernels describe the sensitivity of the model towards each of these measurements. It does not describe the sensitivity towards the traveltime of one particular (ray-theoretical) phase. The kernel computation formalism ensures that the proper sensitivity for each window and filter is computed, whatever they may be, meaning a time window containing triplicated waves can be used just as any other time window. One should just not expect a ray-theoretically intuitive meaning corresponding to each measurement.

The calculation of full wavefields in a laterally heterogeneous 3-D Earth model is still prohibitively expensive for frequencies above 0.05 Hz. Hence waveform tomography must currently choose between one of two compromises:

1. In a laterally heterogeneous Earth model, calculate low frequency wavefields (< 0.05 Hz), since high frequencies are not affordable. This means focusing on surface waves and the low-frequency part of body waves. Due to the large wavelengths of body waves, their low-frequency part offers little resolution in the mantle transition zone (already at a dominant period of 20 s, the kernel fills the entire transition zone). The high cost of wavefield calculations mandates that they need not be done too often. The adjoint method proposed by Tanerola (1984), and applied in continental-scale seismology by Tromp et al. (2005), Fichtner et al. (2009) and Zhu et al. (2012), offers an efficient solution by calculating wavefields only once per source, resulting in composite, so-called event kernels, which indicate the descent direction for the (linearised) gradient search. Several iterations are possible and customary, since wavefields can be computed in arbitrary Earth models, in particular also the updated ones.

2. In a spherically symmetric Earth model, calculate kernels that span any or all parts of the seismically relevant frequency spectrum. This broadband capacity has defined “finite-frequency tomography” since Dahlen et al. (2000). Nissen-Meyer et al. (2007b) showed that full wavefield kernel computations are feasible for frequencies up to 1 Hz, due to the extreme computational savings that result from smart exploitation of the spherical symmetry. The use of high-frequency waves promises accordingly higher image resolution. The method is so efficient that all source-to-receiver kernels are explicitly calculated, turning the problem into one of matrix inversion, for which powerful analysis concepts and computational tools are well known. The disadvantage is that several iterations are not possible, since the Earth model would lose its spherical symmetry after the first update. This might be a serious drawback in media with heterogeneity of strong magnitude, where the single-scattering (Born) approximation starts breaking down, but where several linearised iterations might still lead significantly closer to the global misfit minimum than a single one.

We believe that the finite-frequency approach is currently better suited to tomography of the upper mantle and the transition zone, since (a) being able to use the highly resolving body waves across their entire frequency range should be a big advantage, and (b) all previous studies let us expect only relatively weak perturbations from a layered background model like IASP91, on the order of a few percent, so that the single-scattering approximation should be completely adequate.

A global reference model may not be best suited for a regional study. Rather, careful selection of a suitable regional reference model is a crucial step of a tomography.

We note that the mixed use of forward modelling codes (\( WKBJ \), reflectivity method) has historical reasons and reflects an unfinished (though functional) stage of development. Ultimately all steps will be carried out with the most complete method, Axisem. For inversion of source time functions from teleseismic data, \( WKBJ \) has been an efficient tool since Sigloch and Nolet (2006). It is completely adequate for teleseismic waves, and this STF inversion step is treated as independent from the modelling of triplicated waveforms. Reflectivity is used for efficient forward modelling of the triplicated broadband seismograms (\( WKBJ \) cannot easily compute triplicated phases, and Axisem is not yet set up to do true broadband computations efficiently for the number of computations needed). In order to compute sensitivity kernels, the full wavefield is needed, and we obtain it from full numerical forward modelling using Axisem (but not yet routinely up to frequencies of 1 Hz).

Analysis of triplicated waveforms has so far been mostly applied to deep events (Tajima and Grand, 1995; Tajima et al., 2009), in order to separate the influence of the discontinuities from the depth phases. We have shown that shallow events can be modelled when source parameters are carefully estimated. Routine catalogue estimates (Global CMT (Dziewoński et al., 1981) or NEIC) do not deliver all the parameter we need (source time function), or not to the required accuracy (e.g., source depth).

However, using our own source inversion results from teleseismic P-waves, we can model the sources sufficiently well for our purposes. The ability to use shallow earthquakes...
enlarges the data base enormously, since most earthquakes occur shallower than 30 km depth. In particular, good tomographic resolution requires good azimuthal coverage by sources, but few regions on Earth are surrounded by subduction zones to generate deep earthquakes from all directions.

The regional data sets are promising, both for North America and for Europe. They will be seamlessly embedded into a global inversion that also contains teleseismic P-wave measurements Sigloch (2011). A regional tomography of Europe can thus still benefit from events in eastern Asia, i.e. beyond the triplicated range. Hence the fact that the regional seismicity around Europe is weaker than in North America, is compensated by the superior azimuthal coverage at teleseismic distances. Nevertheless, the European network is nowhere as dense as the USArray, which will make any American mantle structure far better resolved in the foreseeable future. Average waveform cross-correlation is poorer in the European data set than in the North American one. Three possible explanations come into mind:

1. Station quality might be lower. We do not believe this is generally the case, even though the average distance to the nearest coast is smaller in Europe than in North America.

2. European mantle structure could be more complicated than under Northern America, generating a larger mismatch between observed and modelled waveforms. The tectonic history of Europe is often thought to be more complex, but tomographic studies since the advent of USArray have also revealed very heterogeneous mantle structure under North America (Pavlis et al., 2012; Becker, 2012). Hence it is unlikely that the true seismic velocity structure in the mantle under Europe deviates significantly more from a layered model than under North America.

3. Earthquake sources around Europe may be less suited. We think this is the main issue. In North America, we can use rather strong strike-slip events along the west coast, and numerous deep events along the Guerrero subduction zone, many of them exceeding magnitude 6. European seismicity is weaker in magnitude and tends to consist of complicated events in the Aegean subduction and along the Anatolian fault; strike-slip events along the Atlantic ridge are rather weak. Since some of these events are not contained in the IRIS WILBER archive and thus only the ORFEUS stations were available to us, our source inversion for them might be more error prone as well.

The seismic section from the Mexican earthquake demonstrates the high signal quality of USArray recordings (Fig. 10). The discussed strong imprint of a depressed 660 in this signal shows that we may need to be careful to properly parametrize the inversion such that depressed or elevated discontinuities are detected and become part of the tomography result, rather than smearing into bulk velocity structure. In order to separate the two effects, we are considering the use of boundary topography kernels (Colombi et al., 2012), in addition to the volumetric velocity kernels shown in Fig. 5.

6 Conclusions

We conclude that regional body waves should be usable and useful for waveform tomography. We plan to invert these data using finite-frequency tomography and kernels from full numerical wavefield computations (Nissen-Meyer et al., 2007b), but our conclusions about the nature of the data have broader validity.

After careful deconvolution of the source time function and other source parameters from teleseismic waveforms, we obtain good cross-correlations between observed and modelled triplicated seismograms, across the broadband range and even for shallow sources. Due to the much more complex nature of the waveforms, these fits are lower than what we obtain for teleseismic P-waves, but are still sufficient to assemble two decently sized tomography data sets for North America and Europe. The inclusion of these data greatly increase and complement the sensitivity to transition zone structure, and in particular to the discontinuities at 410 km and 660 km, which so far must be investigated using waves of far lower signal-to-noise ratio. The abundance and high quality of data from USArray may the transition zone under North America the natural target for a first waveform inversion using triplicated P-waves.

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