Periodicity in the BrO/SO$_2$ molar ratios in the volcanic gas plume of Cotopaxi and its correlation with the Earth tides during the eruption in 2015

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Abstract. We evaluated NOVAC (Network for Observation of Volcanic and Atmospheric Change) gas emission data from the 2015 eruption of the Cotopaxi volcano (Ecuador) for BrO/SO$_2$ molar ratios. The BrO/SO$_2$ molar ratios were very small prior to the phreatomagmatic explosions in August 2015, significantly higher after the explosions, and continuously increasing until the end of the unrest period in December 2015. These observations together with similar findings in previous studies at other volcanoes (Mt. Etna, Nevado del Ruiz, Tungurahua) suggest a possible link between a drop in BrO/SO$_2$ and a future explosion. In addition, the observed relatively high BrO/SO$_2$ molar ratios after December 2015 imply that bromine degassed predominately after sulfur from the magmatic melt. Furthermore, statistical analysis of the data revealed a conspicuous periodic pattern with a periodicity of about 2 weeks in a 3-month time series. While the time series is too short to rule out a chance recurrence of transient geological or meteorological events as a possible origin for the periodic signal, we nevertheless took this observation as a motivation to examine the influence of natural forcings with periodicities of around 2 weeks on volcanic gas emissions. One strong aspirant with such a periodicity are the Earth tides. Our central result is the observation of a significant correlation between the BrO/SO$_2$ molar ratios with the north–south and vertical components of the calculated tide-induced surface displacement with correlation coefficients of 47 and 36 %, respectively. From all other investigated parameters, only the correlation between the BrO/SO$_2$ molar ratios and the relative humidity in the local atmosphere resulted in a comparable correlation coefficient of about 33 %.

1 Introduction

Magmatic melts are a reservoir of dissolved volatile species. Typically, the dominant part of those volatiles is water vapour followed by carbon dioxide and sulfur compounds but also a large number of trace gases like halogen compounds. The solubility of volatiles in magmatic melts is primarily pressure dependent with secondary dependencies on temperature, melt composition, and volatile speciation (Gonnermann and Manga, 2013). Monitoring the magnitude and composition of volcanic gas emissions has the potential to give insight into those geological processes which vary the solubility regime within a volcanic system. Because the pressure dependency of the volatile solubility is different for each particular volatile species, molar ratios of major gas constituents in volcanic plumes are discussed as accessible
and suitable proxies for the magma pressure and degassing depth. In particular carbon-to-sulfur (Burton et al., 2007) and halogen-to-sulfur ratios, such as chlorine-to-sulfur (Edmonds et al., 2001) and bromine-to-sulfur (Bobrowski and Giuffrida, 2012) ratios, turned out to be powerful tools sensitive to events of magma influx at depth and the arrival of magma in shallow zones of the magmatic system.

The development of passive remote-sensing techniques such as differential optical absorption spectroscopy (DOAS, Platt et al., 1980; Platt and Stutz, 2008) allows for recording semi-continuous (only during daytime) long-term time series of the magnitudes of volcanic gas emissions as well as analyses of the shape and transport of volcanic gas plumes. Since the early 2000s, the costs of performing such measurements have been drastically reduced due to the installation of automatic remote-sensing networks at an increasing number of volcanoes, e.g. Soufrière Hills (Edmonds et al., 2003), Stromboli and Mt. Etna (Flux Automatic MEasurements (FLAME) network; Burton et al., 2009; Salerno et al., 2009), Kilauea (FLYSPEC; Businger et al., 2015), or White Island (Miller et al., 2006). Most prominently, the Network for Observation of Volcanic and Atmospheric Change (NOVAC, Galle et al., 2010), funded by the European Union in 2005, encompasses today about 100 automatically measuring optical UV spectrometers at 41 volcanoes, which are predeterminedly located in South and Central America. The NOVAC data are recorded by UV spectrometers which scan across the sky from horizon to horizon in steps of 3.6° by means of a small field-of-view telescope yielding a mean temporal resolution of about 10 min per scan. The usable wavelength of the recorded spectra ranges from 280 to 360 nm, which allows – in its current state – for an automatized retrieval of the volcanic trace gas concentrations of SO2 (Galle et al., 2010) and BrO (Lübcke et al., 2014) in the volcanic gas plumes.

The utilization of BrO/SO2 molar ratios as a proxy for volcanic activity has several benefits but also drawbacks in terms of data uncertainty and error sources when compared to SO2 emission fluxes. First of all, the accuracy of SO2 emission flux estimates may experience high uncertainties due to the atmospheric radiative transport (e.g. Mori et al., 2006; Kern et al., 2010), relies on the quality of wind data used to approximate plume speed, and requires additional information on plume altitude. In contrast, the BrO/SO2 molar ratios are at most indirectly dependent on the plume speed and plume position, and the radiative transport effects approximately cancel out (Lübcke et al., 2014). On the other hand, while SO2 is directly emitted from the volcano and is assumed to have a lifetime of hours to days (e.g. Beirle et al., 2014; Fioletov et al., 2015), volcanic bromine is considered to be predominately emitted as hydrogen bromine (HBr) and is only partially converted by photochemistry to BrO by the so-called bromine explosion process (e.g. Platt and Lehrer, 1997; Wennberg, 1999; von Glasow, 2010). The equilibrium of the conversion HBr ← BrO is typically reached already within the first minutes after the release of HBr to the atmosphere (Platt and Bobrowski, 2015; Gliß et al., 2015). The NOVAC instruments (typically installed 5–10 km downwind of the crater and thus observing plumes with an age of about 10–30 min) scan through volcanic gas plumes which are expected to have already reached the BrO equilibrium. The conversion rate or even the stationary state ratio between HBr and BrO may depend on plume composition and atmospheric conditions (meteorology) (Roberts et al., 2014) and thus on parameters such as solar irradiance, air temperature, air pressure, and relative humidity. However, Bobrowski and Giuffrida (2012) have not found a correlation between BrO and the relative humidity or the wind speed, which poses the question of whether the bromine explosion in volcanic gas plumes is indeed significantly dependent on the meteorological conditions or not.

The large data set of more than 10 years of semi-continuous time series of volcanic SO2 emission fluxes as well as time series of the BrO/SO2 molar ratios allows for a statistical investigation of long-term signals in the volcanic degassing and comparisons with other long-term signals or a comparison between different volcanoes. The Earth tidal forcing might cause such a long-term signal in the volcanic degassing data. First studies from Stoiber et al. (1986) and Connor et al. (1988) hypothesized about a possible tidal impact on the observed SO2 emission fluxes at Masaya and Kilauea, respectively. The NOVAC data allow us to reinvestigate this hypothesis with a much larger database. Conde et al. (2014) observed a periodic pattern of roughly 13 days in the NOVAC SO2 emission fluxes from Turrialba which was suggested by the authors to be caused by a pressure change due to the Earth tidal forcing. Bredemeyer and Hansteen (2014) used NOVAC data from Villarrica and Llaima to investigate a possible correlation between their SO2 emission fluxes and the surface displacement due to the Earth tides and reported correlation coefficients of up to 20 and 30 %, respectively. In this paper we retrieve the variation in the BrO/SO2 molar ratios recorded by NOVAC during the 2015 period of unrest at the Cotopaxi volcano (e.g. Bernard et al., 2016; Gaunt et al., 2016; Morales Rivera et al., 2017) and examine their correlation with variations in local meteorological conditions and partial components of synthetic ground surface displacements obtained from an Earth tide model.

2 Cotopaxi

2.1 Geology and volcanism at Cotopaxi

Cotopaxi (−0.7° S, 78.4° W; 5897 m a.s.l.) is a glacier-capped stratovolcano located in the Ecuadorian inter-Andean valley, a N–S to NNE–SSW trending topographical depression. Volcanism in this area is caused by the oblique subduction of the Nazca plate beneath the South American plate, which experiences intense large-scale deformation leading to shortening of the lithosphere along the Andean orogeny.

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Figure 1. Time series of the vertical (a, and red line in b) and horizontal (blue and green lines of b) components of the ground surface displacement at Cotopaxi due to the Earth tides. (a) Hourly resolved vertical surface displacements (black, left ordinate axis) and its daily peak-to-peak variation (red, right ordinate axis). (b) Time series of the daily peak-to-peak variation for all three spatial directions. Vertical and east–west components of the tide are in phase and have a periodicity of 14.8 days. The north–south component of the tide has no strictly regular periodicity but reaches a maximum roughly every 13–14 days and increases from September to December 2015.

(e.g. Trenkamp et al., 2002; Alvarado et al., 2016). The volcano lies on a fault transfer zone (e.g. Gibbs, 1990) in which E–W-striking normal faults and NNE–SSW-striking vertical, right–lateral oblique strike-slip faults accommodate the differential crustal shortening rates encountered north and south of Cotopaxi (Fiorini and Tibaldi, 2012). Fiorini and Tibaldi (2012) thus proposed that the fault planes and restraining bends of this transfer zone act as the main magma pathways feeding the volcano. Observations of ground deformation and hypocentre distributions of volcanic earthquakes made in 2001/02 (Hickey et al., 2015) and 2015 (Morales Rivera et al., 2017) suggest that Cotopaxi currently has a shallow magma reservoir beneath the southwestern flank, which is located at a depth of approximately 5–12 km below the summit. Within the last 0.5 Ma, a rhyolitic and andesitic bimodal magmatism has occurred at Cotopaxi (Hall and Mothes, 2008). The Smithsonian Institution (http://volcano.si.edu/) lists 55 eruptions at Cotopaxi within the last 300 years, with the last confirmed eruption in 1940 (VEI 2) and an unconfirmed eruption in 1942 (VEI 3) and the last major (VEI 4) eruption in 1877. The major hazard of an eruption from Cotopaxi consists in the generation of lahars as a consequence of the melting the snow and ice at the summit glacier (Barberi et al., 1995). During the 1877 eruption the glacier of Cotopaxi was melted completely by the expelled pyroclastic flows, producing devastating lahars which travelled down the flanks of the volcano and destroyed, e.g., the town of Latacunga located about 30 km south of the volcano (Aguilera et al., 2004). Later activity of Cotopaxi did not involve melting of the glacier, which has thus recovered since then.

2.2 Predicted Earth tidal surface displacement at Cotopaxi location

The tidal forces periodically displace the Earth’s surface and interior; a summary of the theory of the Earth tides can be found in Appendix A. The periodicities and magnitudes of the tide-induced surface displacement patterns at Cotopaxi are plotted in Fig. 1 (predicted with the GNU R software using the package from Gama and Milbert, 2015). The vertical surface displacements vary by up to $\pm 0.3$ m within a day and follow a semi-diurnal periodicity (Fig. 1a, hourly resolved data). The semi-diurnal peak-to-peak variation (calculated as the maximum difference within a sliding window of 13 h) of the vertical surface displacements varies between 0.15–0.55 m with a maximum every 14.8 days (Fig. 1a, red line). For ocean tides, this long-term periodicity is called spring–neap tidal cycle, a labelling which we adopt in this paper also for the Earth tides, i.e. maximum daily variations during a spring tide and minimum daily variations during a neap tide. Notably, each second spring tidal maximum is slightly more pronounced because the tide-inducing forces of Moon and Sun are slightly stronger during a full moon, than they are during new moon. The Earth tides also result in horizontal displacements (see Fig. 1b). Near the equator, where
Cotopaxi is located, the east–west displacement is a factor of 5 and the north–south displacement is a factor of 10 smaller than the vertical displacement, but for higher latitudes these ratios differ. The east–west component of the tide is in phase with the vertical component (see also Fig. 5) while the north–south component has no strictly regular periodicity but reaches a maximum roughly every 13–14 days. This is mainly due to the elliptic shape of the Moon’s orbit and the inclination of the Earth with respect to the ecliptic. Furthermore, due to the variation in the solar declination all tidal components display a semi-annual modulation of the mean displacement with maximum (for the vertical and east–west component) or minimum (for the north–south component) variation at the autumnal and vernal equinox (around 23 September and 20 March, respectively).

2.3 Cotopaxi’s recent unrest and eruption

In early April 2015 the seismic event rate started to increase, and this marked the beginning of a new period of unrest. From mid-May 2015 onwards, the observed volcanic degassing of SO$_2$ and BrO also increased to significant levels above the detection limit. On 14 August 2015 several phreaticmagmatic explosions opened the conduit resulting in continuous ash emissions and large gas emissions. The period of unrest and eruptions was monitored by the broad network of different sensors maintained by the local observatory Instituto Geofísico, Escuela Politécnica Nacional (IGEPN) in Quito which published the accumulated data as well as interpretations in scientific papers. These publications discussed the comparison of the temporal variations in magnitude (Bernard et al., 2016) and the composition (Gaunt et al., 2016) of ash emissions as well as ground deformation (Morales Rivera et al., 2017) with seismic signals, SO$_2$ emission fluxes, and general visual observations. Morales Rivera et al. (2017) reported a maximum uplift of 3.4 cm at the western flank of Cotopaxi from April to August 2015, while they observed no further significant deformation after the eruption in August 2015. The authors explain the deformation by an inclined sheet intrusion located a few kilometres southwest of the summit. Bernard et al. (2016) and Gaunt et al. (2016) agree regarding the division of the post-explosion dynamics into four phases: 14 to 15 August (phase 1), 15 August to 2 October (phase 2), 2 October to 4 November (phase 3), and 4 to 11 November (phase 4). In phase 1, several phreaticmagmatic explosions occurred, which generated ash clouds reaching altitudes of 9.3 km above the crater and strong gas emissions. During phase 2, continuous but decreasing ash emissions were observed. In the first half of phase 2, the number of seismic long-period events as well as the amplitude of tremor was the highest of the overall period of unrest. In Phase 3, tremor and magnitude of ash emissions increased again and peaked in the middle of October. In phase 4, only little ash was emitted and the ash plumes did not exceed 2.5 km above the crater.

Gaunt et al. (2016) suggest an intrusion of juvenile magma into a shallow reservoir (less than 3 km depth) since April 2015 as the reason for the reawakening of Cotopaxi, a sug-
gestion backed by the findings of Morales Rivera et al. (2017). The juvenile magma may have started to heat an overlying hydrothermal system which may have ultimately resulted in dry degassing pathways, an interpretation which fits the observation of shallow \( \text{SO}_2 \) degassing from May 2015 on. The phreatomagmatic explosions removed the plug which consisted of old, altered material. After the explosions, the magma ascent slowed down and/or the residence times at shallow levels increased. As the crystallinity increased, the magma stiffened and a new shallow plug was formed. The authors further highlighted that the fragmentation mechanisms during phases 2 to 4 are not fully understood. Especially the continuous fine ash grain size distribution throughout all phases suggests that several fragmentations took place. As a possible interpretation, the authors suggest a repetitive formation and destruction of shallow plugs.
Table 1. Typical SO$_2$ SCDs and BrO SCDs in the gas plume of Cotopaxi in the year 2015. Except for the first time period, the mean values refer to the data which are filtered for the strong plume threshold SO$_2$ SCD $> 7 \times 10^{17}$ molec cm$^{-2}$.

<table>
<thead>
<tr>
<th>Time period (in year 2015)</th>
<th>Mean SO$_2$ SCD</th>
<th>Max. SO$_2$ SCD</th>
<th>Mean BrO SCD</th>
<th>Max. BrO SCD</th>
<th>Mean BrO/SO$_2$</th>
</tr>
</thead>
<tbody>
<tr>
<td>1–22 May</td>
<td>$1 \times 10^{17}$ molec cm$^{-2}$</td>
<td>$2 \times 10^{17}$ molec cm$^{-2}$</td>
<td>$\approx 0$</td>
<td>$4 \times 10^{13}$ molec cm$^{-2}$</td>
<td></td>
</tr>
<tr>
<td>22 May–14 Aug</td>
<td>$1 \times 10^{18}$ molec cm$^{-2}$</td>
<td>$2 \times 10^{18}$ molec cm$^{-2}$</td>
<td>$2 \times 10^{12}$ molec cm$^{-2}$</td>
<td>$7 \times 10^{13}$ molec cm$^{-2}$</td>
<td>$0.2 \pm 0.1 \times 10^{-5}$</td>
</tr>
<tr>
<td>14–22 Aug</td>
<td>$2 \times 10^{18}$ molec cm$^{-2}$</td>
<td>$3 \times 10^{18}$ molec cm$^{-2}$</td>
<td>$2 \times 10^{13}$ molec cm$^{-2}$</td>
<td>$8 \times 10^{13}$ molec cm$^{-2}$</td>
<td>$1.1 \pm 0.2 \times 10^{-5}$</td>
</tr>
<tr>
<td>22 Aug–8 Sep (data gap)</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>8 Sep–5 Dec</td>
<td>$1 \times 10^{18}$ molec cm$^{-2}$</td>
<td>$1 \times 10^{19}$ molec cm$^{-2}$</td>
<td>$2 \times 10^{14}$ molec cm$^{-2}$</td>
<td>$4 \times 10^{14}$ molec cm$^{-2}$</td>
<td>$4.8 \pm 1.8 \times 10^{-5}$</td>
</tr>
<tr>
<td>5 Dec–1 May 2016</td>
<td>$1 \times 10^{18}$ molec cm$^{-2}$</td>
<td>$2 \times 10^{18}$ molec cm$^{-2}$</td>
<td>$4 \times 10^{13}$ molec cm$^{-2}$</td>
<td>$1 \times 10^{14}$ molec cm$^{-2}$</td>
<td>$4.4 \pm 1.6 \times 10^{-5}$</td>
</tr>
</tbody>
</table>

3 DOAS measurements of SO$_2$ and BrO

3.1 NOVAC stations at Cotopaxi

Today four NOVAC stations are installed around Cotopaxi at distances of 2 to 15 km, predominantly downwind (Fig. 2). The stations Refugio (instrument no.: D2J1260) and NASA (I2J4969) have operated since 2008. In August 2015, the instrument I2J4969 was relocated from NASA station to the more distantly located new San Joaquín station because the former became unsuitable due to increased ash precipitation. In October 2015, the stations Refugio Sur (D2J2815) and Cami (D2J2835) were additionally installed.

3.2 SO$_2$ and BrO time series during the Cotopaxi 2015 period of unrest

We used DOAS in order to retrieve SO$_2$ and BrO gas emissions from NOVAC data taken during the Cotopaxi period of unrest and eruption (May 2015–April 2016). Our evaluation is based on Lübcke et al. (2014) but with a modified plume detection algorithm and the option to switch the SO$_2$ fit range when extreme SO$_2$ emissions are observed (see for both issues Appendix B). The output of the evaluation are time series of the slant column densities (SCDs) of SO$_2$ and BrO as well as time series of the daily averages of the BrO/SO$_2$ molar ratio in the centre of the volcanic gas plume. SO$_2$ SCDs are the raw data which, combined with information on the plume expansion and the wind conditions, allow the calculation of SO$_2$ emission flux estimations. Accordingly, under stable meteorological conditions (similar plume extension and wind speed) SO$_2$ SCDs and SO$_2$ fluxes are highly correlated and share similar long-term behaviour.

From August 2015 to February 2016, Cotopaxi also emitted large amounts of ash. These ash emissions can alter the atmospheric radiative transport and thus result in an underestimation of the retrieved SCDs (e.g. Mori et al., 2006; Kern et al., 2010). Nevertheless, those underestimations are approximately the same for both gas species; thus, their ratio is almost not affected by those ash emissions (Lübcke et al., 2014). Further, it is under debate whether ash has a different scavenging effect on sulfur and halogens (Bagnato et al., 2013; Delmelle et al., 2014).

Based on marked changes in degassing activity, we divide the SO$_2$ and BrO time series into five time periods (1 to 22 May 2015, 22 May to 14 August 2015, 14 to 22 August 2015, 8 September to 5 December 2015, and 5 December 2015 to 1 May 2016). Characteristic results for these time periods are summarized in Table 1.

Prior to May 2015, Cotopaxi was limited to fumarolic degassing and no significant gas plume was detected since the installation of the NOVAC instruments in 2008 (SO$_2$ SCDs $\leq 2 \times 10^{17}$ molec cm$^{-2}$ and BrO SCDs were below the detection limit of $3 \times 10^{13}$ molec cm$^{-2}$, i.e. twice the standard deviation; Fig. 3a and b). Between mid-May 2015 and the phreatomagmatic explosions on 14 August 2015 the SO$_2$ SCDs increased by up to $2 \times 10^{18}$ molec cm$^{-2}$ and the BrO SCDs increased by up to $7 \times 10^{13}$ molec cm$^{-2}$. Within this period, the calculated BrO/SO$_2$ molar ratios were extremely low with an average of $0.16 \pm 0.13 \times 10^{-5}$ (Fig. 3c). No variations can be resolved because the values are close to the BrO detection limit.

Within the week directly after the phreatomagmatic explosions on 14 August 2015, mean SO$_2$ SCDs of $2 \times 10^{18}$ molec cm$^{-2}$ were observed with a maximum value of $3 \times 10^{18}$ molec cm$^{-2}$, the mean BrO SCDs increased from approximately 0 to $2 \times 10^{13}$ molec cm$^{-2}$ to a maximum of $8 \times 10^{13}$ molec cm$^{-2}$, and a mean BrO/SO$_2$ molar ratio of $1.1 \pm 0.2 \times 10^{-5}$ was derived. From 22 August to 8 September 2015, there are only sparse plume data recorded because the solar panel at NASA station was temporarily covered by ash and the gas plume was apparently not transported through the field of view of the Refugio station during this period. After 8 September 2015, a drop in the SO$_2$ SCDs derived from the data measured at the NASA and San Joaquín stations (green dots in Fig. 3) is expected independently from a possible variation in the volcanic degassing behaviour. The reason is the relocation of the instrument to a larger distance from the emission source; it therefore observes a more diluted volcanic gas plumes.

From early September 2015 to the middle of December 2015, the mean SO$_2$ SCDs remained approximately on the same level as directly after the explosions (significant
amount of data above $1 \times 10^{18}$ molec cm$^{-2}$ but typically below $3 \times 10^{18}$ molec cm$^{-2}$, however with a strong temporal variability (compared to the emission before September 2015) with a maximum of $13 \times 10^{18}$ molec cm$^{-2}$. In contrast, much higher BrO SCDs were observed in this period, with daily maxima typically varying between 1 and $2 \times 10^{14}$ molec cm$^{-2}$ but by up to $4 \times 10^{14}$ molec cm$^{-2}$. As expected with respect to the gas plume dilution, an inter-comparison of the data obtained from the different stations reveals that the observed SCDs in both SO$_2$ and BrO are larger the closer the station is to the edifice of Cotopaxi; however, all stations observed similar BrO/SO$_2$ molar ratios. Further, Refugio station, which is installed just 2 km north of Cotopaxi, observed some extreme SCD values (simultaneously for SO$_2$ and BrO) which are not at all observed by the other stations. A comparison with the wind profile (see also Fig. 4) revealed that at least three (on 29 September, 9 October, 20 October) of those seven SO$_2$ peaks (with SO$_2$ SCDs $> 7 \times 10^{18}$ molec cm$^{-2}$) coincide with extremely low wind speeds ($< 2$ m s$^{-1}$); thus on those days the elevated SCDs may be caused by an accumulation of the volcanic gas emissions in proximity to the crater. Accumulated gas plumes are expected to have a reduced BrO/SO$_2$ molar ratio due to the limited lifetime of BrO. For the three mentioned days, the mean BrO/SO$_2$ molar ratios indeed dropped to $2 \times 10^{-3}$; thus, despite the observed large BrO SCDs, we have to be cautious when interpreting the BrO/SO$_2$ molar ratios of those days. Within the period from early September 2015 to early December 2015 a mean BrO/SO$_2$ molar ratio of $4.8 \times 10^{-5}$ but with variations within $1-12 \times 10^{-5}$ was observed. Further, the BrO/SO$_2$ molar ratios increased from early September 2015 onwards with a trend of about $0.3 \times 10^{-5}$ per month.

Since early December 2015 the mean SO$_2$ SCDs dropped to levels comparable to those prior to the explosions, however, with some minor SO$_2$ degassing events which were detected exclusively by the Refugio station. Also, the mean BrO SCDs dropped to $1 \times 10^{13}$ molec cm$^{-2}$, i.e. below the detection limit; however, in contrast to the situation prior to the explosions for most days, daily maxima above the detection limit were observed with values as high as $1 \times 10^{14}$ molec cm$^{-2}$ on a few days. Around March 2016 we observed some strong gas expulsions approaching SO$_2$ SCDs, which exceeded $7 \times 10^{17}$ molec cm$^{-2}$. The corresponding BrO/SO$_2$ molar ratios were about $4.4 \times 10^{-5}$, and thus similar to the post-explosion value in September 2015. Despite the reliability of this observation being limited due to the small sample size, these data points indicate that the long-term average value of the BrO/SO$_2$ molar ratios was about $4-5 \times 10^{-5}$ during this period.

### 3.3 Periodic pattern in the BrO/SO$_2$ molar ratios after the explosions

Within the time interval from early September 2015 to early December 2015, the highly significant BrO absorptions and the up to four NOVAC stations simultaneously monitoring emission yield an extraordinarily good temporal resolution of the BrO/SO$_2$ time series of almost daily resolution. Therefore, besides the monotonous long-term trend, “high-frequency” (with periods of weeks or months) variations can also be resolved in the BrO/SO$_2$ data. And indeed, the maxima and minima of the BrO/SO$_2$ molar ratios apparently follow a periodic pattern with a period of about 2 weeks and an amplitude (of the smoothed data) of about $1 \times 10^{-3}$, i.e. a relative variation of about 20%, as illustrated by the running mean over 7 days (thick black line in Fig. 3c).

In order to examine a quantitative estimation for the reliability of this signal, we tested two statistical methods: a Lomb–Scargle frequency component analysis (Lomb, 1976; Scargle, 1982; Press et al., 1992; in the following just called Lomb–Scargle analysis) as well as a temporal auto-correlation analysis. Compared with a common Fourier transform analysis these two methods can handle time series with irregular sampling intervals more appropriately, a problem we face as long as we do not interpolate the BrO/SO$_2$ molar ratio time series for the missing days. The Lomb–Scargle analysis is similar to a Fourier transform analysis but explicitly designed for the examination of irregularly spaced time series, and while the auto-correlation analysis still requires a linear interpolation of the BrO/SO$_2$ time series the distortion on the correlation coefficients is much weaker than for a Fourier transform analysis based on sinusoidal signals. Both methods were applied to the daily data (arithmetically averaged over all instruments when daily means were available for several instruments) for the time interval from 8 September 2015 to 15 December 2015 (as illustrated by the black line of the running mean in Fig. 3c). The first week of September 2015 and the first week of December 2015 were excluded from both analyses as the temporal resolution is much worse at those times. Also, the trend was removed by subtracting a polynomial fit to the fifth order from the BrO/SO$_2$ time series. (This should however not be confused with the trend shown in Fig. 3c, which just serves to guide the eye. Nevertheless, the numerical values of both these trend fits are comparable for the time interval from September to December 2015.)

The Lomb–Scargle analysis identifies a periodicity of 13.7 days, and the auto-correlation analysis confirms the existence of a periodicity of 13–14 days (Fig. 3d and e). For both methods, the results are highly significant (Lomb–Scargle false alarm probability of 0.9% and an auto-correlation detection confidence of about 90%), and thus there is a high probability that the periodic signal is an observation of a natural process (or a series of these) rather than statistical noise. At lower confidence levels, the Lomb–
Scargle analysis identifies further peaks at a periodicity of 7.1, 9.7, and 18.8 days.

4 Meteorological conditions during the Cotopaxi eruption

The atmospheric chemistry and meteorological conditions may have an impact on the BrO/SO₂ molar ratios observed in volcanic gas plumes (see introduction). Unfortunately, direct measurements of the meteorological conditions at volcanoes, and in particular at the altitudes of volcanic plumes, are scarcely or not at all available. A quantification of the sky cloudiness or the aerosol load in a volcanic plume may be retrieved directly from the spectroscopic data by well-established methods such as an analysis of variations in the oxygen dimer O₄ absorption or an analysis of the so-called colour index (Wagner et al., 2014). However, the spectra recorded by NOVAC do not allow for an application of the validated versions of these methods because the spectral properties are optimized for a retrieval of SO₂ and BrO, thus for a wavelength range below 360 nm. In contrast, the O₄ analysis requires spectra of good quality also at longer wavelengths. Analyses with modified versions of those methods (see Appendix B4) did not find any reliable pattern in the time series of the sky cloudiness.

Weather forecast models pose the best available proxy for the meteorological conditions around the volcanic gas plume. We use operational analysis data from ECMWF (on a Gaussian grid N640 and with a T1279 truncation) with a spatial resolution of 0.14° × 0.14° and a temporal resolution of 6 h (00:00, 06:00, 12:00, and 18:00 UTC) and picked the meteorological variables at a model altitude around 6000 m a.s.l.
(100 m above the crater, where we roughly expect the volcanic gas plume) in order to get a rough idea of the meteorological variation at the Cotopaxi volcano. From the list of available model parameters, we selected (1) the air temperature, the air pressure, and the relative humidity in order to investigate their possible influence on plume chemistry; (2) the wind speed and wind direction in order to reconstruct the plume transport (and therefore plume age); and (3) the total cloud cover as a poor but still most suitable proxy for the radiative conditions. The total cloud cover gives a relative value (from 0 to 1) for the cloud thickness above a pixel integrated from the ground up to an altitude of 60 km. However, a total cloud cover of 1 does not necessarily indicate the presence of an optically dense cloud cover close to the ground but rather indicates whether significant light scattering within clouds has occurred somewhere above the ground pixel. At the equator, where Cotopaxi is located, the total cloud cover is typically close to 1. For our comparison of gas and meteorological data, we chose to focus on the data obtained at 18:00 UTC, i.e. 13:00 LT, which match the observation time of the DOAS measurement the best, especially when we compare them with the daily averages of the BrO/\(\text{SO}_2\) molar ratios which are centred around noon time.

During the period of unrest, some of the meteorological parameters experienced strong but irregular variations (Fig. 4). We applied a Lomb–Scargle analysis and an auto-correlation analysis to the de-trended time series, which were obtained by subtracting a polynomial fit of the fifth order from the time series. When applied to the presented meteorological time series (1 July 2015 to 1 January 2016), no persistent periodic patterns were detected. When limiting the analysis to the time interval of the investigated BrO/\(\text{SO}_2\) data (i.e. from 8 September 2015 to 15 December 2015), both the variations in relative humidity and cloud cover show noticeable periodic patterns. The relative humidity was at its half-year minimum of 10 % in mid-September 2015 and increased to its half-year maximum of 96 % in the middle of October 2015/early November 2015. Further, this trend was superimposed by a significant (Lomb–Scargle: false alarm probability of 1.2 %) periodicity of 13.1 days. The total cloud cover was at its half-year minimum of 0.6 in mid-September 2015 and increased to its half-year maximum of (persistently) 1.0 early November 2015. Further, for the time interval from September 2015 to December 2015, a periodicity of 11.6 days was proposed (Lomb–Scargle: false alarm probability of 2.2 %). An auto-correlation analysis confirms the existence of the three noted periodicities, all with a confidence of about 90 %. For the other parameters no significant periodic patterns were detected.

5 Discussion

A variation in the BrO/\(\text{SO}_2\) molar ratios in the volcanic gas plume could be caused by effects in two independent domains: either within the magmatic system, i.e. varying magmatic processes could cause a variation in the HBr/\(\text{SO}_2\) molar ratio within the volcanic gas emissions, or in the atmosphere where the atmospheric conditions may delay or accelerate the conversion from HBr to BrO or even change the chemical steady-state ratio between HBr (or other bromine compounds) and BrO.

We observed three significant variations in the BrO/\(\text{SO}_2\) data: (1) an abrupt increase in the molar ratios in September 2015 (unfortunately the exact behaviour is hidden by the data gap), (2) an increasing trend from September 2015 to December 2015, and (3) the periodic pattern from September 2015 to December 2015. In the following we compare the variations in the volcanological, meteorological, and calculated tidal data with the variations in the BrO/\(\text{SO}_2\) data. For the time interval from 8 September 2015 to 15 December 2015, we performed a correlation analysis between the BrO/\(\text{SO}_2\) data, the meteorological data, and the calculated tidal data. We compared the daily averages of the gas data (calculated from data exceeding the strong plume threshold indicated in Fig. 3a), the data around noon of the meteorological data, and the shifted (see below) tidal data. All data sets were left with their long-term trends in order to compare the total variations (see Fig. 5). An analogue analysis with trend-corrected data led to similar results but lower correlation coefficients.

5.1 Comparison of BrO/\(\text{SO}_2\) time series with gas emission rates and meteorology

The BrO/\(\text{SO}_2\) molar ratios are not correlated with the daily means of the \(\text{SO}_2\) slant column density (correlation coefficient of −10 %; see Fig. 5) but are partially correlated with the daily means of the BrO slant column densities (39 %). It is interesting to note that similar observations can be made when comparing BrO/\(\text{SO}_2\) molar ratios and \(\text{SO}_2\) emission rates obtained from the same instruments. For this purpose a time series of the \(\text{SO}_2\) emission rates was provided by Silvana Hidalgo and her colleagues from IGEPN, who have access to a novel wind model with enhanced temporal and spatial resolution allowing for the calculation of more accurate emission rates. A publication of the respective time series of the \(\text{SO}_2\) emission rates is in preparation. Based on the IGEPN data, BrO/\(\text{SO}_2\) molar ratios and \(\text{SO}_2\) emission rates are not correlated during the period of unrest.

When limiting the analysed time interval to early September 2015 to mid-December 2015, relative humidity, total cloud cover, air temperature, and wind speed show long-term variations (Fig. 4); however, these are superimposed by strong short-term variations. For the relative humidity, a frequency analysis finds a significant high-frequency signal with a 13.1-day periodicity which matches relatively well the 13.7-day periodicity of the BrO/\(\text{SO}_2\) data. A cross-correlation analysis of the limited time interval finds a slightly increased correlation coefficient of 33 %. For air temperature, air pressure, and wind conditions, no signifi-
significant periodicities were found and the periodic pattern in the total cloud cover (period of 11.6) does not match with the BrO/SO₂ variations. As a conclusion, the BrO/SO₂ variations may be partially explained by the variations in the relative humidity. However, on the other hand, the correlation between the relative humidity and the BrO/SO₂ molar ratios may just be caused by a shared dependency on, e.g., the Earth tidal forcing (see good correlation between relative humidity and tide-induced surface displacement in Fig. 5).

5.2 Comparison of the BrO/SO₂ time series with the Earth tides

It should be kept in mind that one can expect a delay between a tide-driven process in the volcanic system and the finally observed volcanic gas emissions. We determined the delay by a cross-correlation analysis between the BrO/SO₂ molar ratios and the calculated tidal surface displacement. For this purpose, we shifted the time series of the Earth tide data variably by up to 2 weeks backwards in time and thereby manually maximized the cross-correlation coefficient between BrO/SO₂ and tide-induced surface displacement. However, the optimal delay is different when we optimize for the different components of the tidal signal: it is 242 h when we optimize with respect to the vertical component (or east–west component, which is perfectly in phase with the vertical component) but 41 h when we optimize for the north–south component. As a result we derived correlation coefficients between the BrO/SO₂ molar ratios and the vertical component or the north–south component of 36 and 47 %, respectively (see Fig. 5, where both optimization scenarios are included). As a last analysis step, we dropped the useful representation (radial, north–south, east–west) of the tide-induced surface displacement but correlated the displacement in variable directions (calculated as the component of the displacement vector in the chosen three-dimensional direction) with the BrO/SO₂ molar ratios. The overall optimum was again found to be strictly horizontal and quite strictly to the north (optimum was 1° NNE but with similarly high correlation coefficients for ±8°) and again with a delay of 41 h.

Figure 5. Correlation coefficients of the different data sets, where “Br/S” is used as abbreviation for BrO/SO₂ molar ratios. The colours indicate the absolute value of the coefficient divided into bins of 10 %. The signs of the correlations are indicated by “+” and “−”. The unity auto-correlations are omitted for better readability. In order to account for the delay between tidal forcing and atmospheric measurement, the time series of the tides was shifted backwards in time prior to the correlation analysis. The figure shows the correlation for a shift of 41 h (left column) and for a shift of 242 h (right column); see text for the derivation of the shifts. For both shifts, the north–south component correlates the strongest with the BrO/SO₂ molar ratios.

Figure 6. Graphical comparison of temporal variations in the BrO/SO₂ molar ratio and the predicted tide-induced surface displacement variation in north–south direction. (a) Comparison of the time series. (b) Scatter plot which illustrates the correlation coefficient of 47 % between both time series; the gradually changing colour of the data points gives the measurement date from red (8 September 2015) to blue (15 December 2015).
The tidal north–south displacement component fits both, the trend and the “skewed” periodic pattern in the BrO/SO$_2$ data, extraordinarily well (Fig. 6a). Further, a scatter plot revealed a highly significant contrast in BrO/SO$_2$ data between small and large semi-diurnal tidal deviations (Fig. 6b).

5.3  Comparison of BrO/SO$_2$ time series with volcanic activity

5.3.1  BrO/SO$_2$ molar ratios as a poorly constrained proxy for volcanic activity

The volatile solubility in magmatic melt can be modelled with a high accuracy for water vapour and carbon dioxide (Gönnermann and Manga, 2013; Oppenheimer et al., 2014) and is also relatively well constrained under diverse and variable conditions for sulfur (e.g. Scaillet and Pichavant, 2005; Moretti and Ottonello, 2005; Lesne et al., 2011; Witham et al., 2012). In contrast, it is more challenging to constrain the halogen behaviour in the melt-fluid phase because of their low abundance in magmatic melt but also because halogens (except fluorine) strongly prefer to partition in the hydrous fluid phase (Bureau et al., 2000). For water-poor magmas, the knowledge is limited to the qualitative observation that halogens typically reach saturation, if at all, at low pressure (Edmonds et al., 2009). For water-rich magmas, the quantitative pressure dependency of the chlorine solubility in the melt-fluid phase is relatively well constrained (e.g. Carroll, 2005; Balcone-Boissard et al., 2016), and some insights into the behaviour of the other halogens have also been gathered by the experimental (e.g. Bureau and Métrich, 2003; Bureau et al., 2010, 2016) or empirical (e.g. Villedent et al., 2005; Kutterolf et al., 2015) derivation of their melt-fluid partition coefficients.

Sulfur and water vapour, and thus also bromine, predominately degas after carbon dioxide. Bromine has a larger partition coefficient than chlorine; thus, it is reasonable that bromine degasses prior to sulfur. Sulfur degasses prior to chlorine (e.g. Aiuppa, 2009); however, it has not yet been determined whether sulfur predominately degases prior to or after bromine. Accordingly, even under the assumption that the HBr/SO$_2$ degassing ratio is purely pressure-dependent, no quantitative deduction of the pressure change could be made based on BrO/SO$_2$ molar ratios. Further, it was even not yet possible to derive the sign of this correlation indirectly by empirical studies of BrO/SO$_2$ molar ratios simultaneously to pressure changes (Bobrowski and Giuffrida, 2012; Lübcke et al., 2014) because of the still limited data sets available. In the absence of an explicit interpretation of the BrO/SO$_2$ molar ratio, at least the reasoning that a change in BrO/SO$_2$ molar ratios is probably caused by a significant change in magmatic conditions appears to be nevertheless a reasonable hypothesis. Several studies on BrO/SO$_2$ molar ratios in volcanic gas plumes revealed that the ratios generally follow the same typical pattern: the ratios are relatively low prior to and during an eruption but are higher at the end of the eruption or during quiescent degassing periods, as e.g. observed at Mt. Etna (Bobrowski and Giuffrida, 2012), Nevado del Ruiz (Lübcke et al., 2014), Tungurahua (Warnach, 2015), and also here for Cotopaxi.

5.3.2  Comparison of BrO/SO$_2$ molar ratios with volcanological data

During the week after the explosions on 14 August 2015, the BrO/SO$_2$ molar ratios remained on a similarly low level (≤ 1 × 10$^{-5}$) as prior to the explosions. The BrO/SO$_2$ abruptly increased to a mean value of about 4 × 10$^{-5}$ during the next 2 subsequent weeks. Gaunt et al. (2016) mentioned that the hydrothermal system might have been drying during those weeks. Accordingly, first bromine predominately partitioned in the hydrous fluid of the hydrothermal system, but after the hydrothermal system dried out the bromine had probably directly partitioned to the gas phase.

The increasing trend in BrO/SO$_2$ from the middle of September 2015 to early December 2015 indicates a slow but continuous change in magma pressure, magma temperature, or composition of the degassing magma body. The possible reasons are manifold. Following Gaunt et al. (2016), the mingling of the old magma with juvenile magma could have continuously changed the effective magma composition. Or, in the case that HBr degasses at higher pressures than SO$_2$, a gradual pressure increase due to, e.g., the formation of a new plug may have resulted in suppressed SO$_2$ degassing. If, by contrast, HBr degasses at lower pressures than SO$_2$, the increasing trend may indicate that the magma has already degassed most SO$_2$, while the magma still holds significant HBr which has yet to degas. The latter interpretation would be supported by the relatively large BrO SCDs but rather small SO$_2$ SCDs since January 2016.

5.3.3  Possible volcanological origins for the periodic pattern in the BrO/SO$_2$ molar ratios

The volcanic unrest and in particular the explosions in August 2015 mark a fundamental perturbation of the equilibrium conditions in the volcanic system. Thus, the observed periodic pattern in the BrO/SO$_2$ data might be a manifestation of a damped and oscillating restoring process of the volcanic system to a new equilibrium. However, the damping of magma motion is rather high, and thus a one-time excitation of the magma column, e.g. by the phreatic/magmatic explosions in August 2015, is unlikely to cause an observable oscillation of six consecutive periods. As another possible explanation, the periodic pattern may have been caused by a chance repetition of six one-time events at equidistant time intervals, e.g. by a repetitive plug formation and destruction as suggested by Gaunt et al. (2016). In any case, even if the interpretation of a repetitive plug formation holds true, the probability that those events happened at equidistant timing...
is expected to be rather low unless the events are triggered by a periodic external forcing. The spring–neap tide cycle of the Earth tides is such a continuous periodic forcing which, at least in principle, continuously varies the magmatic system. Finally, we cannot exclude that the unrest or geometry itself might have led to an accidental periodicity in the activity of 2 weeks which was also completely independent from tidal influence, e.g. a periodic magma intrusion from the deep to the shallow reservoir due to tectonics. However, again, it appears to be unlikely that such an accidental periodicity has a period of just 2 weeks. Thus, of all geological origins, tidal forcing appears to be the best candidate to explain the observed periodic signal in the BrO/SO$_2$ data.

5.4 Interpretation of the periodic pattern in the BrO/SO$_2$ data

The observed periodicity in the time series of the BrO/SO$_2$ molar ratios is superimposed on an increasing trend and a large scatter in the data. The latter highlights the complexity of the interpretation of BrO/SO$_2$ molar ratios, which potentially depends on an unknown number of volcanological and atmospheric mechanisms and the fluctuations of their parameters. Despite the large scattering, we nevertheless found an unexpectedly high correlation between the BrO/SO$_2$ molar ratios, on the one hand, and the Earth tidal forcing or the relative humidity, on the other hand, with correlation coefficients of 47 and 33 %, respectively. Thus, the tidal forcing as well as the relative humidity are the most probable candidates to explain a part of the variability in the BrO/SO$_2$ molar ratios. Accordingly, both mechanisms may independently contribute to the variation in the BrO/SO$_2$ molar ratios at the same time. In the following, we focus on the plausibility of a causality between the BrO/SO$_2$ molar ratios and the north–south component of the tidal forcing, which nevertheless appears to be the best candidate.

Tide-generated pressure and stress variations appear to be negligibly small in comparison to the forces that typically act within magmatic systems (Emter, 1997). However, it has been shown in several cases that the effect of these subtle variations can be amplified and thus may play a crucial role if (1) the system is sufficiently open (McNutt and Beavan, 1984; Sottili and Palladino, 2012) and (2) the geometry of the magma feeding systems and reservoirs allows for a tide-induced periodic deformation (e.g. Patané et al., 1994; Sottili et al., 2007), which additionally may be reflected by a periodic spatiotemporal cumulation of volcanic earthquakes in the excited parts of the system (Rydelek et al., 1988; McNutt, 1999; Custodio et al., 2003). Sottili and Palladino (2012), for example, attributed the cyclic clustering of eruptive activity at Stromboli volcano and its concurrence with the times of the syzygies to the tidal response of well-known tectonic structures causing a periodic magma supply and migration in the shallow parts of the plumbing system.

In this reasoning, the shallow emplacement of magma prior to the phreatomagmatic explosion in August 2015 may have (temporally?) shifted the geometry of the Cotopaxi magma plumbing system from a non-excitable to an excitable state. Additionally, the explosive activity very likely gave rise to a transition from closed-system to open-system degassing and thus made the volcano more susceptible to external influences. Further, combining our results and the interpretation from Gaunt et al. (2016) suggests a possible tide-induced repetitive plug formation and destruction, causing an alternation of “open and almost shut condition” as proposed by Fischer et al. (2002) for explosive activity at Karymsky volcano. All these effects can result in a periodic variation in the pressure regime in the shallow magmatic system, leading to a periodic variation in the volatile solubility in the magmatic melt, which in turn may vary the magnitude and/or composition of volcanic gas emissions.

Tide-induced processes are intuitively expected to strictly follow the periodicity of the strongest tidal long-term pattern, that is the spring–neap tide cycle with period of 14.8 days. The observed periodic pattern of 13.7 days in our BrO/SO$_2$ data, however, matches much better with the temporal intra-day amplitude variation in the north–south component of the tide-induced surface displacement, which follows a rather irregular pattern with maxima occurring roughly every 13–14 days. In other words, BrO/SO$_2$ molar ratios were elevated when the tidal amplitude variations in the north–south direction were most pronounced. Our results accordingly suggest that the volcanic system of Cotopaxi (currently?) is more sensitive to tide-induced stresses acting in the north–south direction rather than to stresses in the vertical and east–west directions.

This interpretation is further supported by the orientation of the local fault system and associated ambient stress field at Cotopaxi, which is located in a transfer fault zone with the greatest principal stress acting in the ENE–WSW direction and the weakest principal stress acting in the north–south direction, i.e. also in a horizontal direction (Fiorini and Tibaldi, 2012). Such a setting favours the intrusion and ascent of magma along east–west-striking planar structures, which is further corroborated by the observation of the inclined sheet intrusion beneath the southwestern flank of the volcano (Morales Rivera et al., 2017). Thus, the additional tide-generated stresses probably have a much higher relative impact, when they act in the direction of the weakest principle stress, i.e. normal to east–west-striking compressible magma pathways when compared to the other directions. Such a directional dependency is indeed well known for the tidal response of inclined planar aquifers, which cross-cut borehole wells. Bower (1983), for example, reported oscillations of water levels in boreholes in Canada, which indicated a strong response to the horizontal component of the semidiurnal M2 tide acting normal to the strike direction of the intersecting aquifers.
6 Conclusions

Previous studies on the volcanic gas plumes of several volcanoes (Mt. Etna, Nevado del Ruiz, Tungurahua) observed relatively low BrO/\(SO_2\) molar ratios prior to volcanic explosions and an increasing trend in BrO/\(SO_2\) molar ratios afterwards. These consistent observations raised the question whether the BrO/\(SO_2\) molar ratios can be interpreted as a precursor of volcanic activity and to what extent these can serve as an indicator of pressure fluctuations in the degassing magma residing at shallow levels of the magma plumbing system. We observed similar behaviour at Cotopaxi during its unrest period in 2015, extending the empirical foundation of this claim. At Cotopaxi, the BrO/\(SO_2\) molar ratios almost vanished prior to the phreatomagmatic explosions in August 2015, were significantly higher after the explosions, and further increased from September 2015 to December 2015. After December 2015, the unrest calmed down, accompanied by a decrease in \(SO_2\) SCDs to a level lower than prior to the explosions; however, the BrO SCDs remained relatively large. The latter observation suggests that bromine degassed at Cotopaxi predominately after sulfur from the magmatic melt.

Furthermore, we observed a periodic pattern with a period of 13.7 days in the BrO/\(SO_2\) molar ratios within the volcanic gas plume of Cotopaxi. Despite the fact that the analysed time interval spans just over six periods of this signal, the statistical significance is unexpectedly high in view of the manifold processes that may potentially influence the molar gas ratio (false alarm probability of 0.9% and detection confidence of about 90%). At first, we examined the variability in the meteorological conditions as an origin for the periodic variation in the BrO/\(SO_2\) molar ratios. We found that the relative humidity exhibits a similar long-term trend as the BrO/\(SO_2\) molar ratios, and the trend was further superimposed for half of the time interval by a periodic pattern with a 13.1-day periodicity. Therefore, the periodic pattern in the BrO/\(SO_2\) data may be partially explained by the variations in relative humidity, with a cross-correlation coefficient of up to 33%. Also, a local repetition of independent one-time events cannot be ruled out from the list of possible origins; however, the probability for these to occur equidistantly in time every 13.7 days is presumed to be low. Therefore, Earth tidal forcing appears to be the most promising explanation for the observed periodical BrO/\(SO_2\) variations, where correlation coefficients of 36 and 47% were found between the BrO/\(SO_2\) molar ratios and the vertical and north-south components of the tide-induced surface displacement, respectively. The observed periodicity of 13.7 days implies a mechanism which is linked to the north-south component of the tides, e.g. an amplification of the oscillation by a north-south displacement of the host rock rather than a mechanism which is linked to the much larger tide-induced vertical displacement.

Whether or not the presented data show a manifestation of the Earth tides or are due to some other cause is difficult to answer as yet as we only observed six consecutive periods. Nevertheless, the NOVAC data set allows us to conduct large-scale statistical analyses on this topic. Thus, long time series at a particular volcano might give a deeper insight into the origin of such signals. Future studies will undertake a global comparison of different volcanoes and might reveal which geological geometries are excitable by the tidal forcing.

**Data availability.** Raw spectral data used to obtain the results presented in this study have been acquired within the NOVAC collaboration. Access to these data is permitted with consent of the respective volcanological observatories that own the source instruments, according to their internal policies for data administration. Please refer to the author list for contact details. Access to the presented meteorological data is possible with an ECMWF licence.
Appendix A: Theoretical background on Earth tides

A1 Tidal harmonics

Gravitational forcing caused by the Moon and the Sun in their interaction with the Earth varies with time. The resulting tidal potential (i.e. the residual gravitational potential) is a function of location and time and depends on all astronomical motions such as orbit, rotation, and precession of the involved bodies. The periodicities of these parameters have been studied for millennia and are well known. Already in the 1880s the tidal potential could be calculated with high precision by a harmonic decomposition (Darwin, 1883; Doodson, 1921), i.e. as a sum of an infinite number of harmonic oscillators with accurately known angular frequencies $\omega_i$ and amplitudes $a_i$. In the literature, the amplitudes of the tidal harmonics are conventionally noted as the (theoretical) vertical displacement $\Delta z_i = a_i \cdot g_{rad} \cdot R_\text{eq}$ of the Earth’s surface at the equator, with respect to the equatorial Earth radius $R_\text{eq} = 6378$ km and the conventional standard gravitational acceleration $g_{rad} = 9.80665$ m s$^{-2}$, caused by the forcing of the particular tidal harmonic (Agnew, 2007). The tidal harmonics with the largest displacement amplitudes are summarized in Table A1. Hereby, the strength of a particular tidal harmonic varies with latitude: the semi-diurnal tides are at a maximum at the equator and the poles but vanish at midlatitudes. The diurnal tides are at a maximum at the midlatitudes but vanish at the equator and poles. The long-term tides are at a maximum at the equator and vanish at the poles.

A2 Tidal potential at the equator (at Cotopaxi)

The diurnal tidal harmonics do not contribute to the tidal potential at the equator. The strongest tidal long-term patterns are therefore caused by the interferences of the semi-diurnal tidal harmonics. The rotation of the Earth gives rise to the principal lunar semi-diurnal tide $M_2$ and the principal solar semi-diurnal tide $S_2$. These two strongest tidal harmonics beat together every 14.77 days, a periodic pattern which is commonly known as the “spring–neap tide cycle”. The elliptical shape of the Moon’s orbit causes a modulation of the spring–neap tide cycle with additional beats every 27.55 days ($N_2 + M_2$) and every 9.61 days ($N_2 + S_2$), resulting in an alternation of the spring tidal amplitude (see Fig. 1). The inclination of the Earth’s orbit with respect to the ecliptic (contribution of the lunisolar semi-diurnal tide $K_2$) entails a further modulation of the tidal signal with additional beats every 13.66 days ($K_2 + M_2$), every 182.62 days ($K_2 + S_2$), and every 9.13 days ($K_2 + N_2$). The most obvious impact of $K_2$ is the semi-annual modulation ($K_2 + S_2$) of the spring–neap tide cycle. The beat periodicities of all these interferences of semi-diurnal tidal harmonics are matched by long-term tidal harmonics with identical periodicities, e.g. $M_2 + K_2$ and the lunisolar fortnightly tide $M_f$. The beats and the long-term harmonics interfere; however, except for $M_f$, the amplitudes of the long-term harmonics are rather small compared to the beats of the semi-diurnal harmonics.

The tidal potential results in a displacement of the Earth’s ground surface in all three spatial directions. At the equator, the tide-induced displacement is strongest in the vertical component, weaker in the east–west component, and weakest in the north–south component (see Fig. 1b). The vertical and the east–west component of the tide-induced displacement follows the modulated spring–neap tide cycle. In contrast, the north–south component follows a rather irregular pattern approaching maximum displacement rates roughly every 13–14 days. The discrepancy in beat rate can be explained by the relative impact of the tidal harmonics exerting differential crustal strains in different spatial dimensions. In particular, if the Earth would not be tilted with respect to the ecliptic, there would be no displacement in north–south direction at the equator. Accordingly, the north–south displacement is more sensitive for those tidal harmonics which contribute due to the inclination of the Earth, which is primarily $K_2$. In this reasoning, the tidal harmonics with the strongest north–south component are $K_2$ and $M_2$; thus, the dominant long-term pattern has a beat of 13.66 days ($K_2 + M_2$) rather than the spring–neap tide cycle. The irregularities in the beat rate of the north–south component may be manifestations of the interferences $N_2 + M_2$, $N_2 + S_2$, and $N_2 + K_2$. Furthermore, the north–south component also follows the semi-annual modulation $K_2 + S_2$.

The compartments of the Earth respond differently to the temporal changes in tidal potential according to their mechanical properties such as their viscosity and compressibility. Solid rock is displaced by about 0.2980 (radial Love number of the Spherical, Non-Rotating, Elastic, and Isotropic (SNREI) Earth; see Agnew, 2007) times the theoretical value, e.g. $\pm 0.3$ m at spring tide. In contrast, magmatic melt is a fluid with a higher compressibility than solid rock and may therefore adapt more strongly to the tidal potential. Accordingly, the tidal forcing may lead to a relative displacement between magma in a conduit and the surrounding host rock.

Appendix B: Experimental data: methods and measurement

B1 DOAS and NOVAC

DOAS (differential optical absorption spectroscopy) (Platt and Stutz, 2008) is an analysing technique which is suitable for remote sensing of volcanic gas plumes. The output of DOAS are the simultaneously retrieved slant column densities (SCDs) of a set of volcanic trace gases. The SCDs are the integral of the particle density of the particular gas along the light path. Together with additional information on the expansion of a volcanic gas plume and the wind conditions, the particle density and even the emission fluxes of volcanic
trace gases like SO$_2$ and BrO can be retrieved from the SCDs.
In this paper, we focus on the BrO/SO$_2$ molar ratio in volcanic gas plumes; i.e. none of this additional information is required. At volcanoes, scanning DOAS systems are usually used because these can provide a spatial coverage from horizon to horizon with a good temporal resolution. The instruments in NOVAC were designed in an autarkic and simple set-up in order to match the harsh conditions and remote locations of volcanoes (Galle et al., 2010). As a drawback, NOVAC instruments do not have an active temperature control as the power supply by solar panels is limited. Prior to each scan (≈5–15 min), the measurement routine adjusts the exposure time to the meteorological conditions. As the main goal of NOVAC is the monitoring of volcanic SO$_2$ fluxes, the number of consecutive exposures is manually fixed aiming for the best compromise between precision and temporal resolution of the SO$_2$ measurement. While this leads typically to a precision of the SO$_2$ retrieval in the percent range, the setting is not optimal for the BrO retrieval. Nonetheless, Lübcke et al. (2014) have shown that BrO can also be retrieved from NOVAC instruments by applying an advanced evaluation algorithm. Thus, NOVAC allows us, for the first time, to determine long-term time series of BrO/SO$_2$ molar ratios at a large number of volcanoes.

B2 Retrieval of BrO/SO$_2$ molar ratios from NOVAC data: plume detection and optimizing the BrO detection limit

For all spectroscopic retrievals of SO$_2$ and BrO, we applied the DOAS fit scenarios described by Lübcke et al. (2014), and most evaluation steps were also applied identically. In the first evaluation step, all spectra from a horizon-to-horizon scan are pre-evaluated for SO$_2$ using its particular zenith spectrum as reference spectrum. The result is an SO$_2$-SCD distribution as a function of the viewing angle. While the precision of the SO$_2$ data allows for a spatial analysis of the volcanic plume, the optical density of BrO in a volcanic gas plume is at least 1 order of magnitude smaller than for SO$_2$ and thus a higher photon number contribution is required in order to enhance the signal-to-noise ratio. This is realized by the subsequent addition of spectra which are recorded in the temporal proximity and in the same or at least similar viewing direction.

Accordingly, we used the SO$_2$-SCD distribution to identify all spectra which are predominantly part of the volcanic plume, i.e. with only little dilution, and added the spectra in order to get one “added plume spectrum per scan”. The drawback of this method is the loss of spatial information as the retrieval gives only one mean plume value for the BrO SCDs or the BrO/SO$_2$ molar ratios. A volcanic gas plume can be assumed to have an approximately Gaussian-shaped angular gas distribution embedded in a flat, gas-free reference region. (The reference region might differ from zero SO$_2$ as the arbitrarily picked reference spectrum might contain gas. However, at this stage only the angle-dependent shape and not the quantitative value is of interest.)

For their proof of concept, Lübcke et al. (2014) ignored this reasonable assumption of the plume shape and simply defined the plume region as the angle region (≥33°) with the highest running mean value over 10 spectra for the SO$_2$ SCDs. For relatively narrow volcanic plumes, this fixed plume region may also contain viewing directions where the volcanic plume has been significantly diluted, and therefore the “added plume spectrum” would also contain a significant contribution from the reference region and thus underestimate the SO$_2$ SCD in the real plume. To improve the accuracy, we instead fit a Gaussian distribution to the angular SO$_2$-SCD distribution in order to routinely separate all pure plume spectra from significantly diluted spectra. The 1σ range of the Gaussian distribution is then defined as the plume region. When no or only a partial plume is detected.

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Table A1. Strongest tidal harmonics (Agnew, 2007). The tide species describes its dependency on latitude (see text for details). The Darwin symbols are a set of conventional notation; the amplitude gives the theoretical amplitude of the periodical vertical displacement of the Earth’s surface which would be caused by this particular tidal harmonic alone. The frequency is given in cycles per day, and the length of the period is given in days. The set is divided by the horizontal bars into semi-diurnal, diurnal, and long-term harmonics.

<table>
<thead>
<tr>
<th>Tide species</th>
<th>Darwin symbol</th>
<th>Amplitude (m)</th>
<th>Frequency (cpd)</th>
<th>Length of period (d)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Semi-diurnal tides</td>
<td>M2</td>
<td>0.63221</td>
<td>1.9322736</td>
<td>0.5175251</td>
</tr>
<tr>
<td></td>
<td>S2</td>
<td>0.29411</td>
<td>2.0000000</td>
<td>0.5000000</td>
</tr>
<tr>
<td></td>
<td>N2</td>
<td>0.12105</td>
<td>1.8959820</td>
<td>0.5274312</td>
</tr>
<tr>
<td></td>
<td>K2</td>
<td>0.07991</td>
<td>2.0054758</td>
<td>0.4986348</td>
</tr>
<tr>
<td>Diurnal tides</td>
<td>K1</td>
<td>0.36864</td>
<td>1.0027379</td>
<td>0.9972696</td>
</tr>
<tr>
<td></td>
<td>O1</td>
<td>0.26223</td>
<td>0.9295357</td>
<td>1.075806</td>
</tr>
<tr>
<td></td>
<td>S1</td>
<td>0.12199</td>
<td>0.9972621</td>
<td>1.002745</td>
</tr>
<tr>
<td>Long-term tides</td>
<td>Mf</td>
<td>0.06661</td>
<td>0.0732022</td>
<td>13.66079</td>
</tr>
<tr>
<td></td>
<td>Mm</td>
<td>0.03518</td>
<td>0.0362916</td>
<td>27.55459</td>
</tr>
<tr>
<td></td>
<td>Ssa</td>
<td>0.03099</td>
<td>0.0054758</td>
<td>182.6217</td>
</tr>
</tbody>
</table>

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(concretely, if the Gaussian fit does not succeed or when the 1σ range of the Gaussian fit was less than 5°), the scan is excluded from further analysis. On the other hand, when the 1σ range expands by more than 33° (67% of scans for the presented data), the plume region is defined as by Lübcke et al. (2014). Similarly and in accordance with Lübcke et al. (2014), the 10 spectra of the scan with the lowest SO2 SCDs are considered to be gas-free background spectra and are added together to form one “added reference spectrum per scan”.

In the next step, for each scan, an SO2 and a BrO DOAS fit has been performed based on the added plume spectrum and added reference spectrum. In order to further improve the signal-to-noise of the BrO fits, the added plume spectra of four consecutive scans are added together to form “multi-scan plume spectra”; however, only those scans with \( \chi^2(\text{BrO fit}) < 10^{-3} \) (≈ 95% of all suitable scans) were considered in order to avoid the influence of relatively bad scans. Analogously, also multi-scan reference spectra were obtained. For periods with significant BrO degassing, the final BrO data points have a mean temporal resolution of 10 (and up to ~ 30) data points per day and 1 standard deviation of about \( 3 \times 10^{13} \text{molec cm}^{-2} \). The standard deviation is estimated as 2 times the DOAS fit error of the multi-scan BrO fit (Stutz and Platt, 1996). The SO2 detection limit of the final data is in the order of \( 1 \times 10^{16} \text{molec cm}^{-2} \) (displayed by the dashed line in Fig. 3a); i.e. the precision of the SO2 data is still about a factor of 100 better than for BrO and thus within the scope of BrO/SO2 molar ratio calculation considered to be exactly measured.

The BrO detection limit can be further enhanced by, e.g., daily averaging to dynamic values of \( \text{BrO}^{\text{DT}} = \frac{3}{\sqrt{n}} \times 10^{13} \text{molec cm}^{-2} \leq 1 \times 10^{13} \text{molec cm}^{-2} \) (with \( n \) the number of “multi-scan” data points per day), but in any case, most retrieved BrO SCDs are below the detection limit (displayed by the dashed line in the second panel of Fig. 3 and empty circles in Fig. 3c). However, blindly rejecting all data with BrO SCDs below the detection limit would not only drastically reduce the number of available data but would also select those scans when the BrO SCDs is particularly high. As such a selection leads to systematically overestimated molar ratios, a more careful selection criteria is required for more accurate BrO/SO2 molar ratio calculation (Lübcke, 2014).

As we are not actually interested in the BrO SCDs but the BrO/SO2 molar ratios, we set our criteria in order to increase the reliability of observed (low) molar ratios. For this purpose we define periods of strong degassing as being above an SO2-SCDs threshold level of \( \text{SO2}_{\text{thresh}} = 7 \times 10^{17} \text{molec cm}^{-2} \) and select only those data which are above the threshold. Within those data, the maximum detection limit of the BrO/SO2 molar ratios is \( \text{(BrO/SO2)}^{\text{DT}} = \frac{\text{BrO}^{\text{DT}}}{\text{SO2}_{\text{thresh}}} = \frac{4}{\sqrt{n}} \times 10^{-5} \leq 1 \times 10^{-5} \).

The SO2 threshold is chosen as the best compromise between a low BrO/SO2 detection limit and sufficient amount of data passing the criteria. For observed SO2 SCDs further above the threshold, the BrO/SO2 detection limit also further decreases. As a consequence, some BrO/SO2 data which fluctuate around zero can also pass the selection criteria (i.e. whose BrO SCD is below the BrO detection limit). Following the preceding reasoning, we interpret those data (or at least their long-term averages) as reliable observations of rather low BrO/SO2 molar ratios. In Fig. 3c, we highlighted data above or below the BrO detection limit by full and empty circles, respectively. However, both kinds of data were treated identically in the subsequent analysis steps.

B3 Alternative SO2 fit range for unusually strong SO2 emissions

The approximations which are applied to the DOAS algorithm are only justified for weak absorbers, i.e. if the investigated optical density is below ~ 0.1. For a larger optical density, the DOAS approach usually underestimates the SCD of the investigated trace gas. For the “standard” (i.e. following Lübcke et al., 2014) SO2 fit range from 314.8 to 326.8 nm, SO2 can be considered to be a weak absorber for SCDs of up to ~ \( 1 \times 10^{18} \text{molec cm}^{-2} \), but the SO2 SCD is increasingly underestimated with increasing optical densities. For most NOVAC data, the SO2 SCDs do not exceed this threshold significantly; however, during the Cotopaxi unrest 2015, SO2 SCDs of up to the order of \( 1 \times 10^{19} \text{molec cm}^{-2} \) were observed. For more accurate SO2 SCDs, we re-evaluated the multi-scan plume spectra with an alternative fit range from 326.5–335.3 nm, which was suggested by Hörmann et al. (2013) in order to evaluate SO2 SCDs up to about \( 1 \times 10^{19} \text{molec cm}^{-2} \). As a drawback, the SO2 measurement error is here drastically increased with relative values of about 10%, i.e. about \( 1 \times 10^{18} \text{molec cm}^{-2} \) for the extreme SCDs. In order to pick the most reliable data, we use the results of the standard SO2 fit as a default fit but switch to the “alternative” fit if the discrepancy between both fit results is larger than 4 times the fit error of the alternative fit (thus about 2 times the measurement error of the SO2 SCD; Stutz and Platt, 1996), i.e. if the discrepancy is more than about \( 2 \times 10^{18} \text{molec cm}^{-2} \).

B4 Challenges when applying the oxygen dimer O4 and colour index retrieval to NOVAC data

Established cloud detection algorithms are based on the absorption of the oxygen dimer O4 at 360 nm or the relative intensity ratio of the intensity of the backscattered solar radiation at 320 and 440 nm (see, e.g., Wagner et al., 2014). The application of these or similar algorithms to NOVAC data faces at least three challenges. (1) The effectively detected wavelengths range from 280 to 400 nm, however, with a linear decrease in transmittance already from 370 to 400 nm due to the HOYA U330 UV bandpass filter. Accordingly, the standard colour index pair is not applicable. (2) The measurement routine automatically optimizes the integration time...
of the spectra with respect to the wavelength range of the SO$_2$ retrieval (~310–335 nm). As a drawback, spectra are often oversaturated starting, in particular on cloud-free days, at 365 nm but sometimes even already at 359 nm. Accordingly, the standard O$_4$ retrieval is typically not applicable to NOVAC data when the sky is cloud-free. On the other hand, the absorption signal of the O$_4$ line at 344 nm is not significant for a spatial analysis. (3) Many NOVAC instruments (at Cotopaxi three of four) use a conical scan geometry and thus never record zenith spectra. Missing the zenith value for O$_4$ or the colour index makes the interpretation of the analysis results more challenging.

We nevertheless tested both methods on the NOVAC data retrieved from the Cami station (because there zenith information is available). For the colour index analysis, we compared the mean intensity of the wavelength ranges at 329–329.7 nm and at 381–381.6 nm (each the average of 10 detector channels; see also Lübcke, 2014). We applied the analysis to the zenith spectra of each particular scan. The resulting time series of the colour index has not shown any periodic pattern and most long-term variations were small compared to the mean daily variations (see Fig. B1a). For the O$_4$ retrieval, we applied a fit scenario with the same absorbers as for BrO (see Lübcke et al., 2014) but with a fit range from 338 to 365 nm. We applied the analysis to the individual spectra within each scan and used the particular zenith spectrum as the reference spectrum. A comparison with the results of the SO$_2$ retrieval showed no correlation; i.e. no systematic enhancement or reduction in O$_4$ absorption signal has been observed within the volcanic plume.

As an additional approach, we applied the same O$_4$ analysis to the multi-scan plume spectra recorded by all NOVAC stations at Cotopaxi and used the particular multi-scan reference spectrum as a reference spectrum. The resulting time series neither contained periodic patterns nor showed a significant correlation with BrO/SO$_2$ molar ratios. On the other hand, the stations Refugio and Refugio Sur, where the plume typically passes at lower elevation angles, found O$_4$ enhancements of about $2 \times 10^{42}$ molec cm$^{-2}$ in the plume, while the stations Cami and San Joaquin, where the plume typically passes in about elevation direction, found no O$_4$ enhancement in the plume (see Fig. B1b). This enhancement is probably solely due to the dependency of the background O$_4$ SCD on the elevation angle, illustrating the difficulty of interpreting the O$_4$ results. We want to highlight that more sophisticated and well-validated studies which, for example, make use of massive filtering of the data may indeed retrieve information on the aerosol load from the NOVAC data; however, the development of such a sophisticated cloud classification algorithm is beyond the scope of this study.
Competing interests. The authors declare that they have no conflict of interest.

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